

# Evolving Local Fuzzy Models to Adapt in a Dynamic Environment: An Example in Asset Management

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**imagination at work**



# Outline

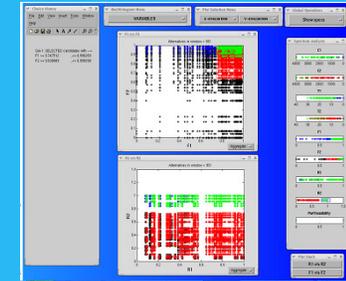
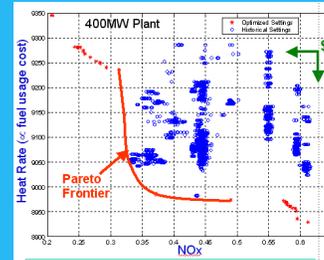
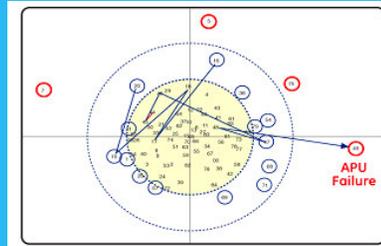
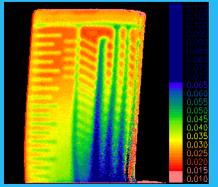
1. PHM at GE Global Research
2. Issues in Model Lifecycle
3. Computational Intelligence and Model Generation
3. Fuzzy Instance Based Model (F-IBM)
4. Prediction of Best Units for Asset Selection: Case Study
5. Future Work

# 1. PHM at GE Global Research

- PHM Technical Synergies
- PHM Elements
- PHM Installed Basis
- PHM Technology

# PHM Technical Synergy

## Prognostics and Health Management (PHM)

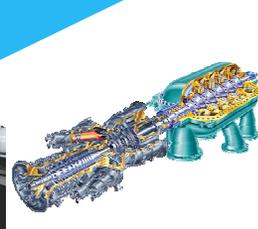
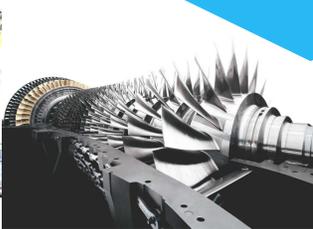


On-board Sensors  
& Off board  
Inspections

Anomaly Detection,  
Diagnostics &  
Prognostics Alg.

On-board /  
Off board  
Optimization Alg.

Visualization &  
Multi-Criteria  
Decision-Making  
Systems



GE Healthcare

GE Aviation

GE Energy

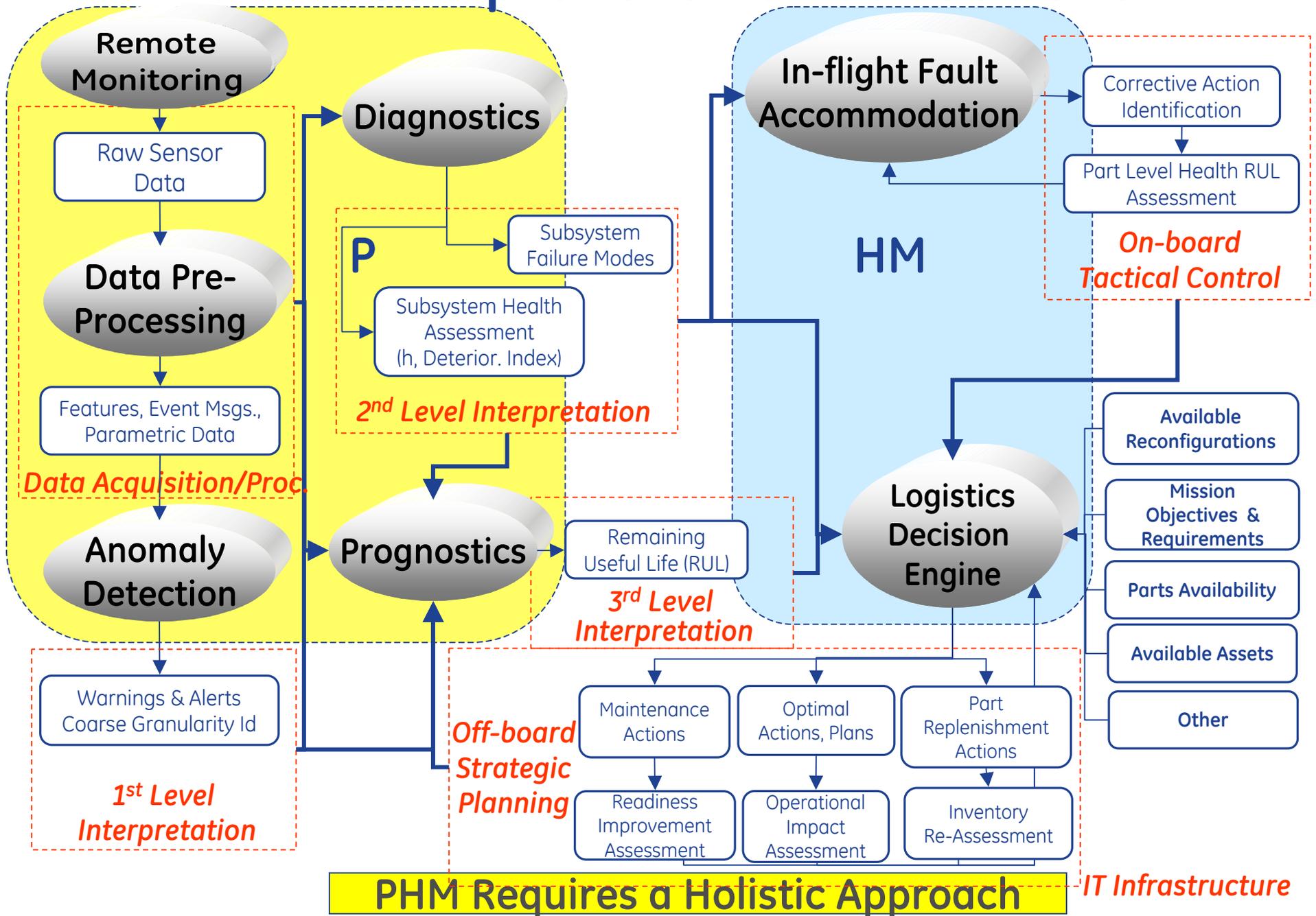
GE Oil & Gas

GE Rail

LM

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# PHM: Comprehensive Foundations



# PHM: From RM&D to Prognostics & Optimization

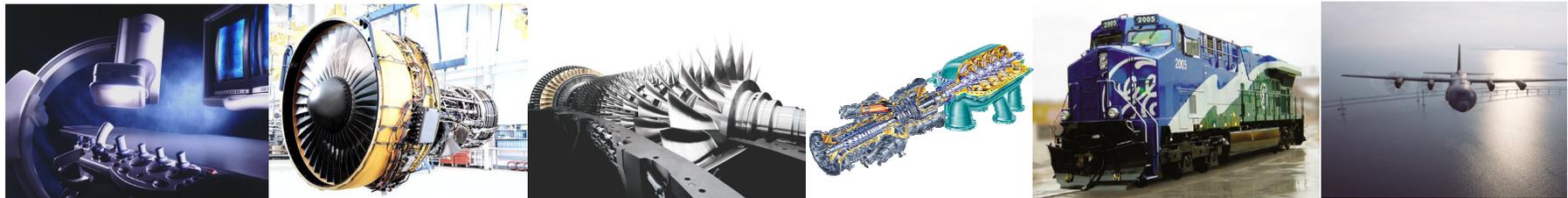
## GE RM&D/PHM Installed Base

~20,000 steam/gas/hydro/wind turbines

~17,500 aircraft engines

~9,000 rail locomotives

~60,000 medical imaging machines



GE Healthcare

GE Aviation

GE Energy

GE Oil & Gas

GE Rail

Lockheed Martin

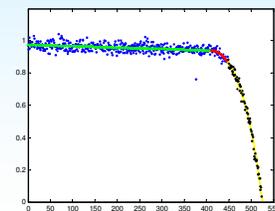
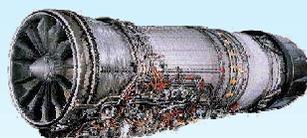
## PHM Elements

### Diagnostics

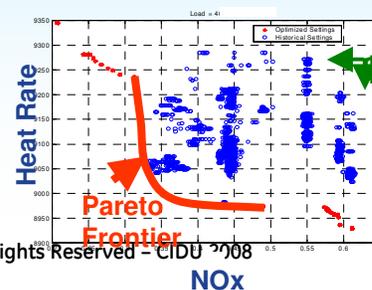


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### Prognostics



### Optimization



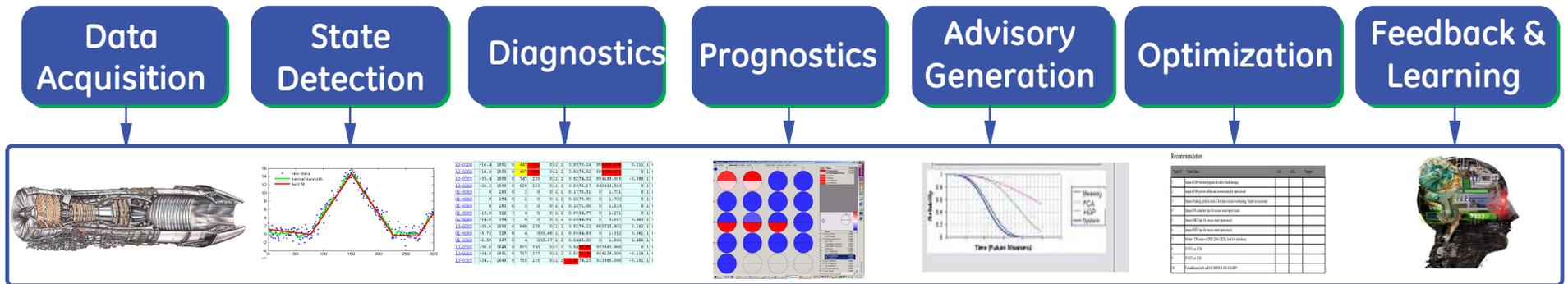
### Maintenance decisionmaking



- Mission Objectives & Requirements
- Parts Availability



# PHM Technologies



## Functions

**On-platform sensors**  
Data recorders  
**Off-platform sensors**  
Inspection / NDE  
Data repository  
Data de-noising  
Data smoothing  
Data compression  
Data transmission  
IT infrastructure

**Features**  
Generation/Selection  
Manual/Automated  
**Anomaly Detection**  
Normal / Abnormal  
structures (trajectory,  
clusters, states, patterns)  
**Anomaly Resolution / Id.**  
Resolving sensors faults,  
op. transients, model  
faults, system faults

**State Interpretation**  
Manual/Automated  
Classification  
**Fault mode Id.**  
**Health Assessment**

**RUL Prediction**  
Manual/Automated  
RUL forecast  
**Health Assessment**  
**Projection**  
**Lifing**  
Fault propagation

**On-board Fault Accommodation**  
**Off-board DSS**

**Maintenance Optimization**  
Workscope (build level)  
Shop scheduling  
**Logistics Optimization**  
Supply Chain Mgmt  
**Operational Optimization**  
Asset/mission allocation

**Performance metrics dashboard**  
**Ground truth acquisition**  
**Structured feedback**

## Key Technologies

Electronics  
Signal Processing  
Communication  
Information Theory  
Statistics  
Nondestructive  
Inspection

Physics-based model  
Machine Learning  
(unsupervised)  
Statistics (Clustering, RF)  
Pattern Recognition  
Information Theory  
Soft Computing  
(NN, Fuzzy, Probabilistic,  
Covariance-based)  
Signal Processing

Physics-based model  
Machine Learning (Sup.)  
Statistics  
(CART, RF, MARS)  
Pattern Recognition  
Soft Computing  
(NN, Fuzzy Classifiers  
Prob. Classifiers)  
AI (case-based,  
rule-based)

Physics-based Lifing (fault prop.)  
Physics-based Model (Cycledeck)  
Machine Learning (Lazy learning)  
Statistics (Kernel-based  
regressions)  
Pattern Rec. (ARMA)  
Soft Computing  
(NN regressions, Fuzzy  
(TS), EA tuned models)  
AI (case-based)  
NDE Inspection

Adaptive control  
EA-designed control  
Human Interface  
Usability  
Multi Criteria DM (MCDM)

Multi-Objective  
Optimization (MOO)  
Evolutionary Algorithms  
Operations Research  
Multi Criteria DM (MCDM)

Automated Performance  
Monitoring  
Supervisory learning

## GR Labs / GE Business [a partial list]

NDT Lab  
Integrated Device Lab  
Communications Lab  
Service Enabled Arch Lab  
GE Aviation Systems

iAI Lab  
Automation & Controls Lab  
GE Aviation Systems

iAI Lab  
Automation & Controls Lab  
GE Aviation Systems

Lifing Technologies Lab  
iAI Lab  
Automation & Controls Lab  
NDT Lab  
GE Aviation Systems

iAI Lab  
Automation & Controls Lab  
Risk and Value Mgmt. Lab

iAI Lab  
Risk and Value Mgmt. Lab.

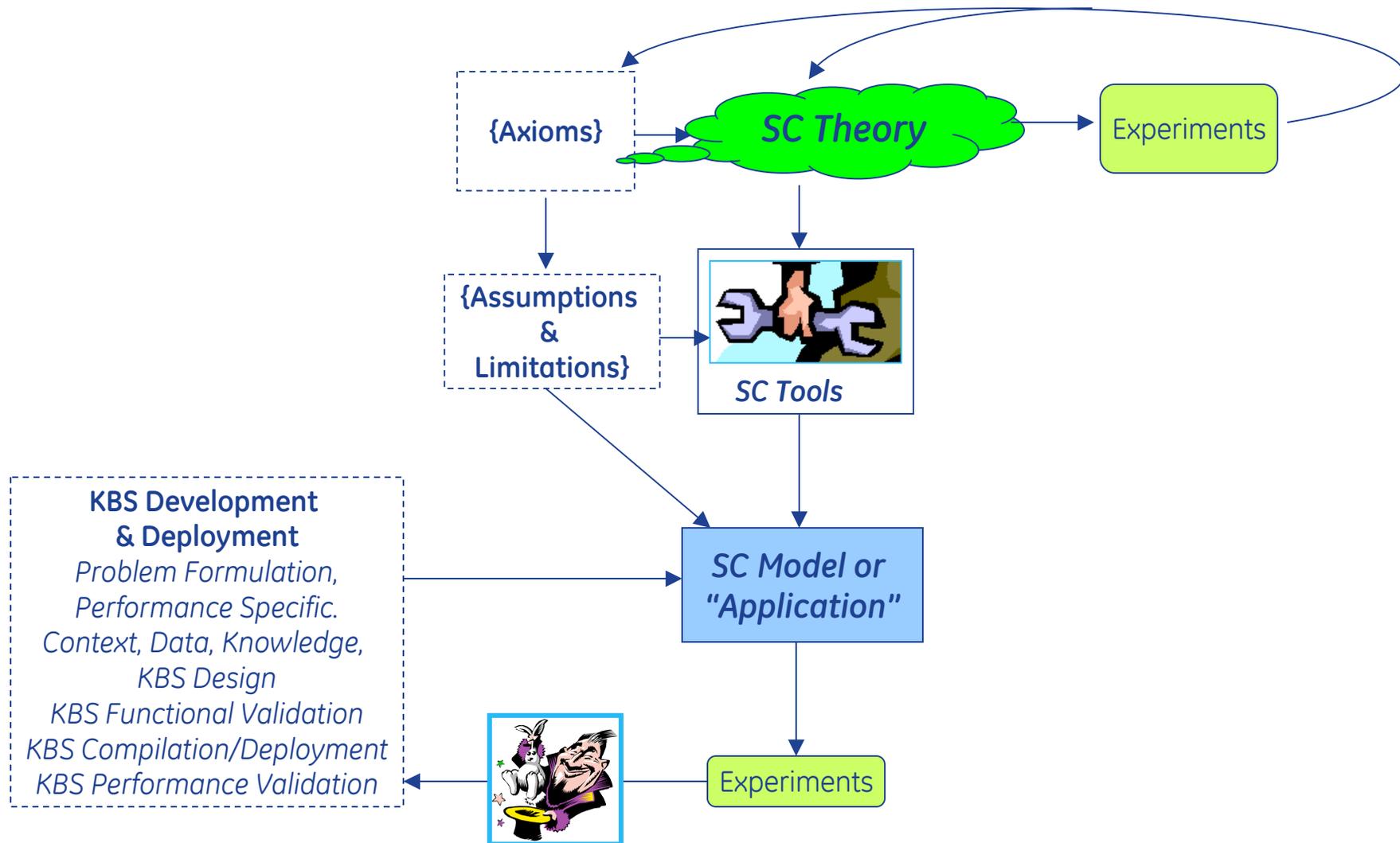
iAI Lab



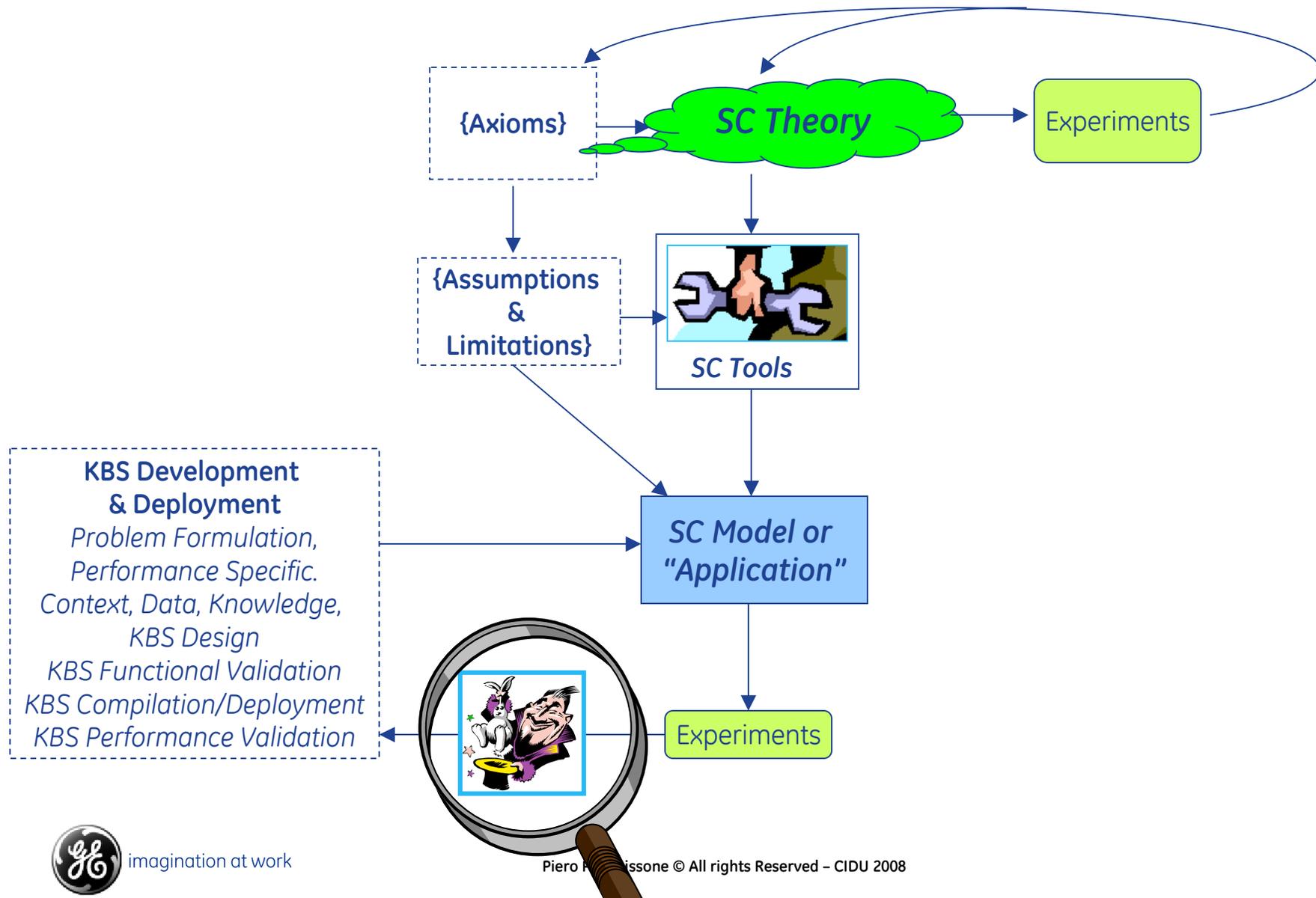
## 2. Issues in Model Lifecycle

- Handcrafting Models
- Lifecycle: Build, Use, Update & Maintain

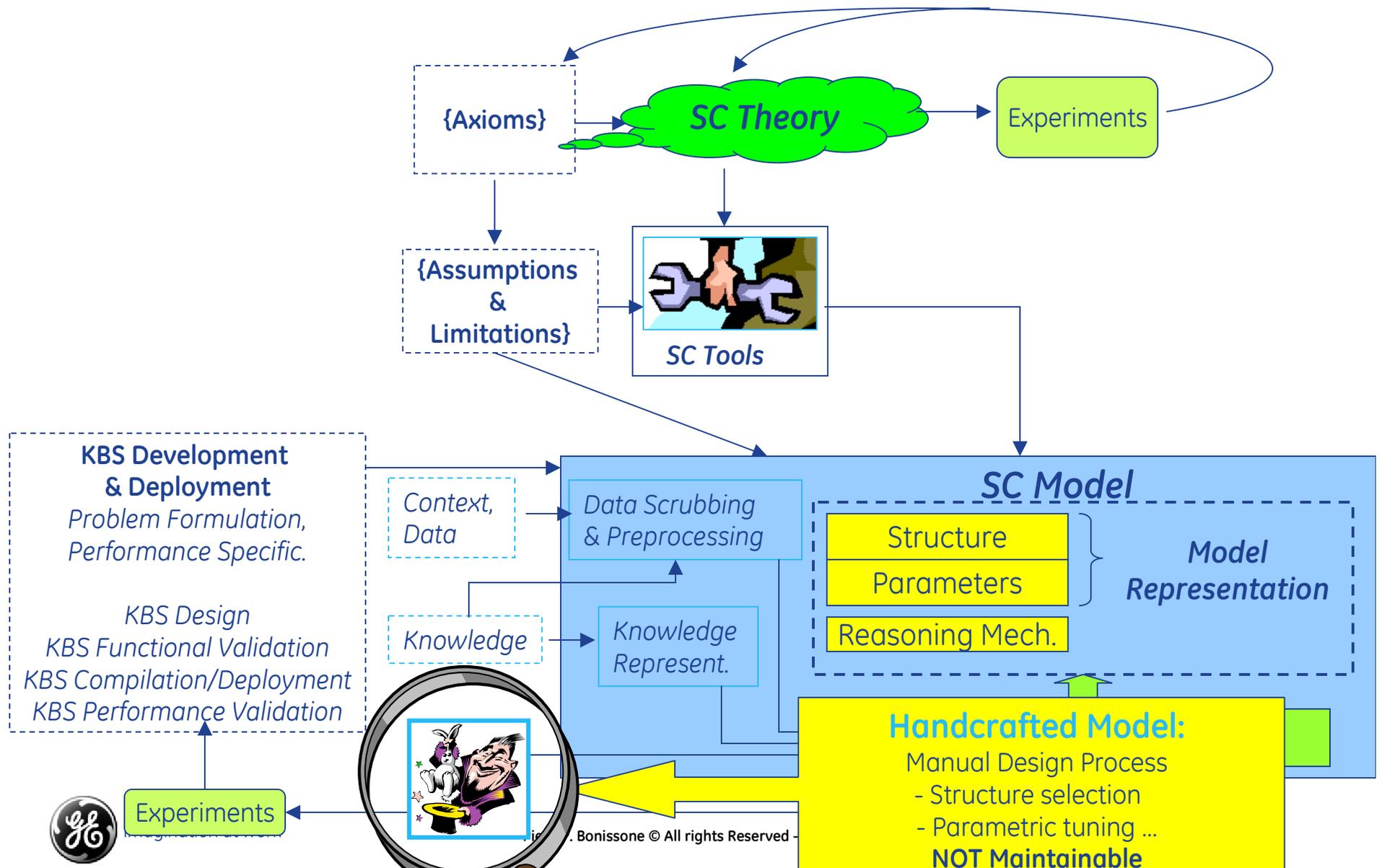
# Model Generation Process: Pictorial



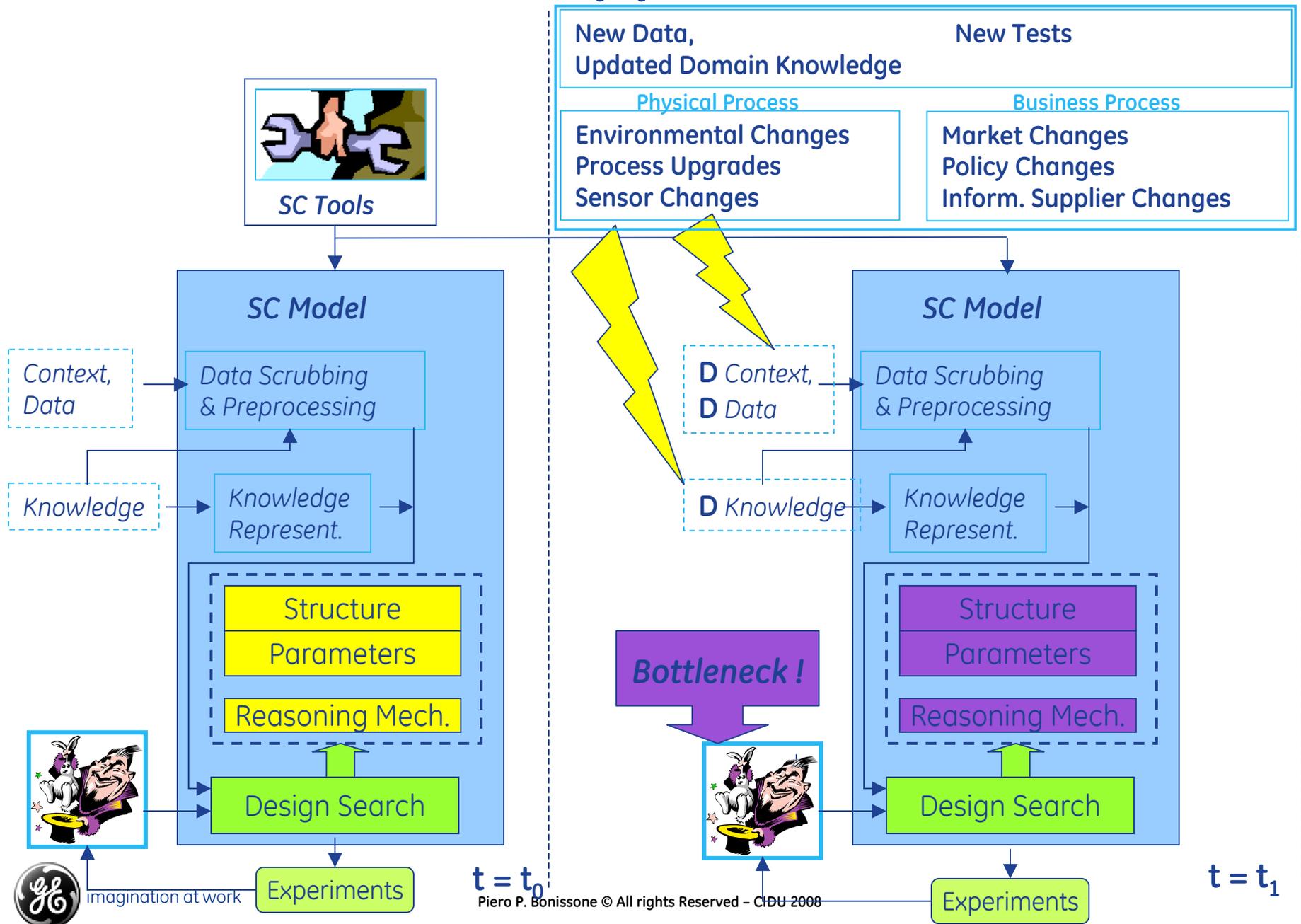
# What is Wrong with this Picture?



# Let's Analyze the Problem

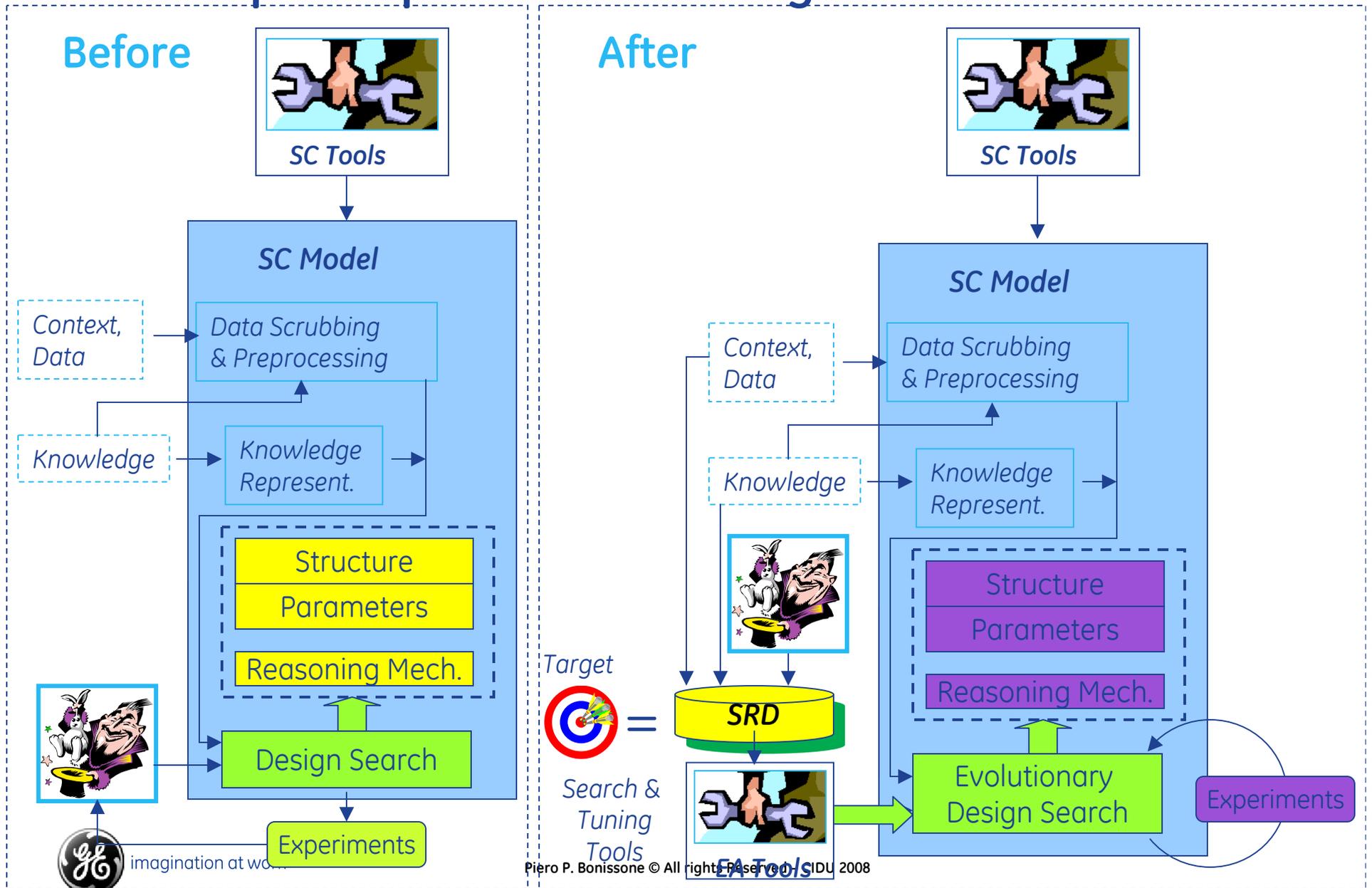


# What Will Happen Over Time?



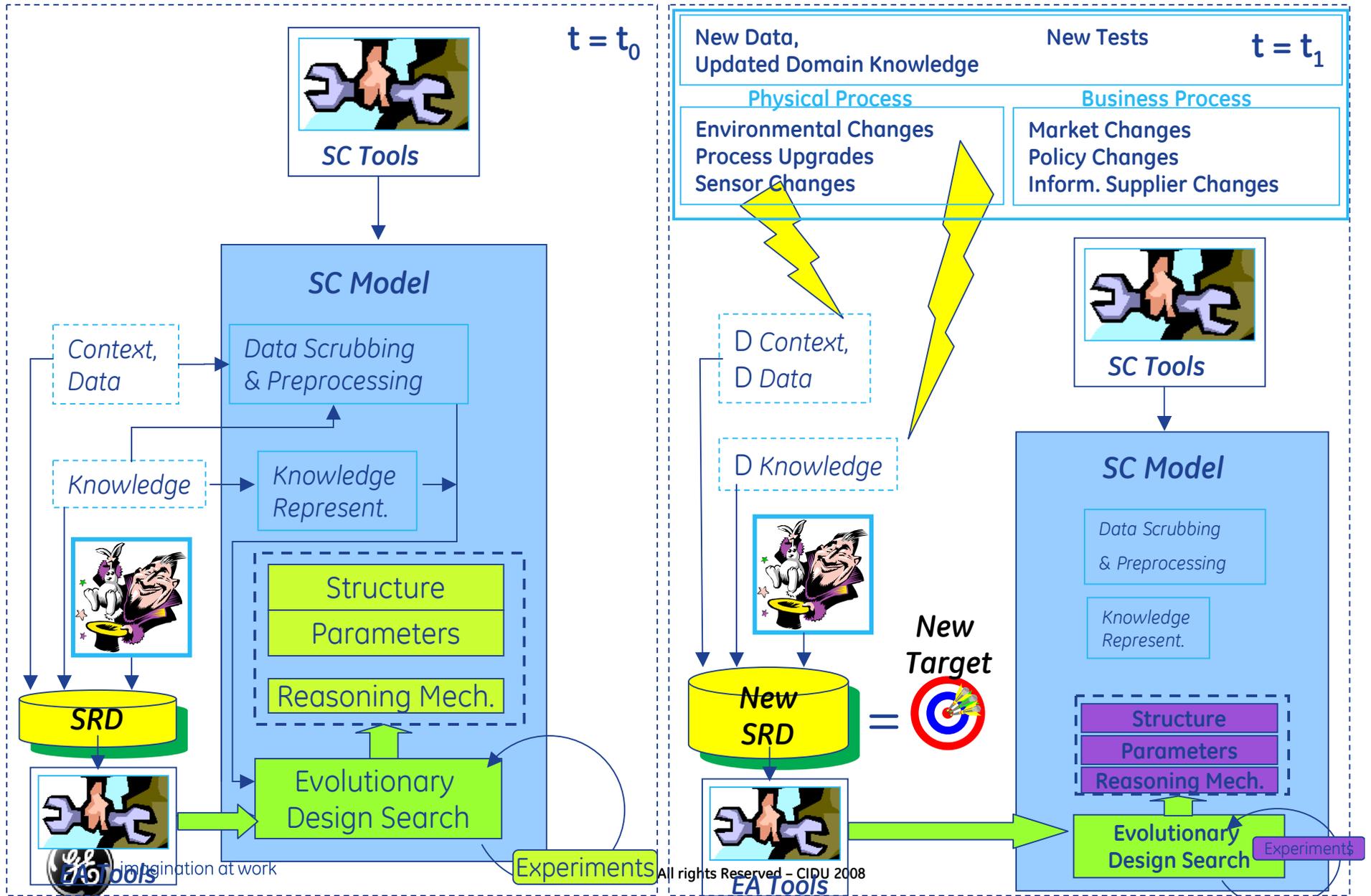
# Addressing the Lifecycle of a KBS

## Example: Supervised Learning



# Addressing the Lifecycle of a KBS (cont.)

## Example: Supervised Learning

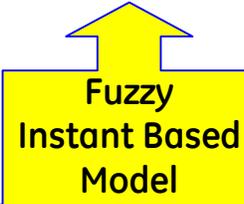


# 3. Computational Intelligence and Model Generation

- Representation, Reasoning, and Search
- Functional Approximation (ANFIS) vs Fuzzy Instance Based Model (F-IBM)

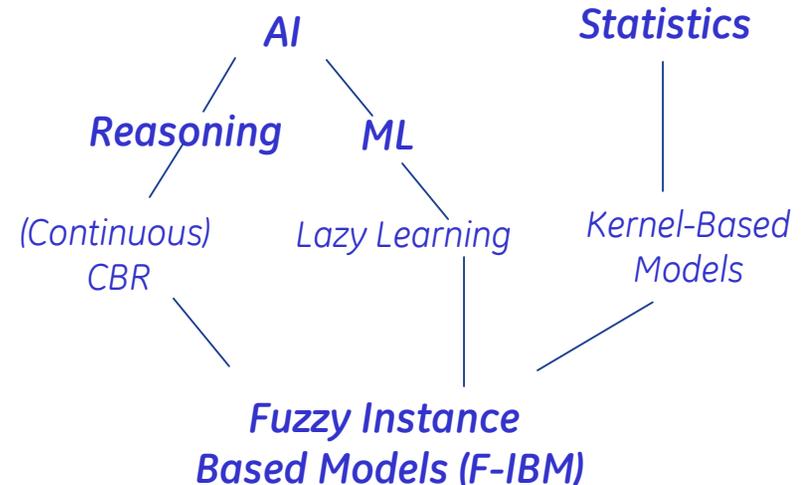
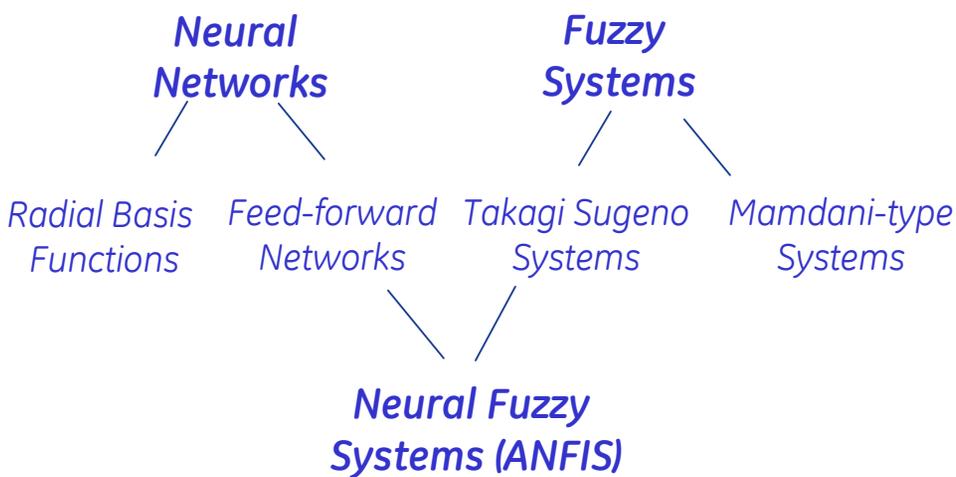
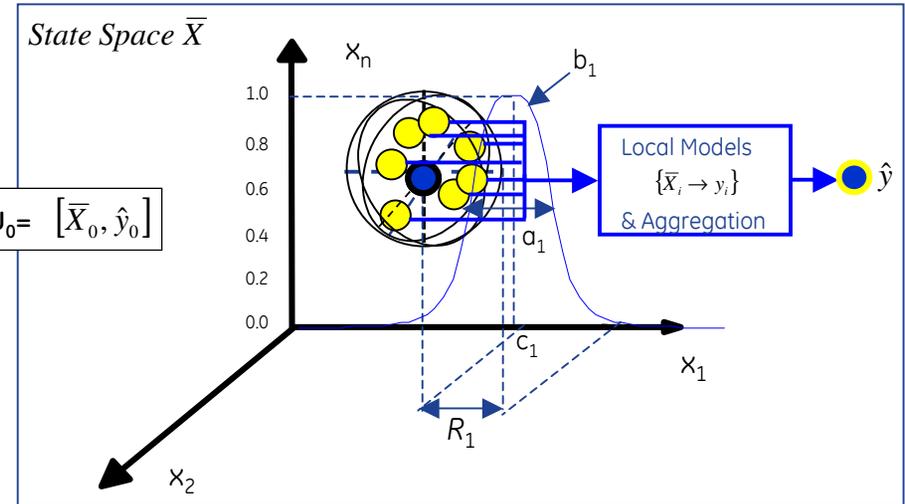
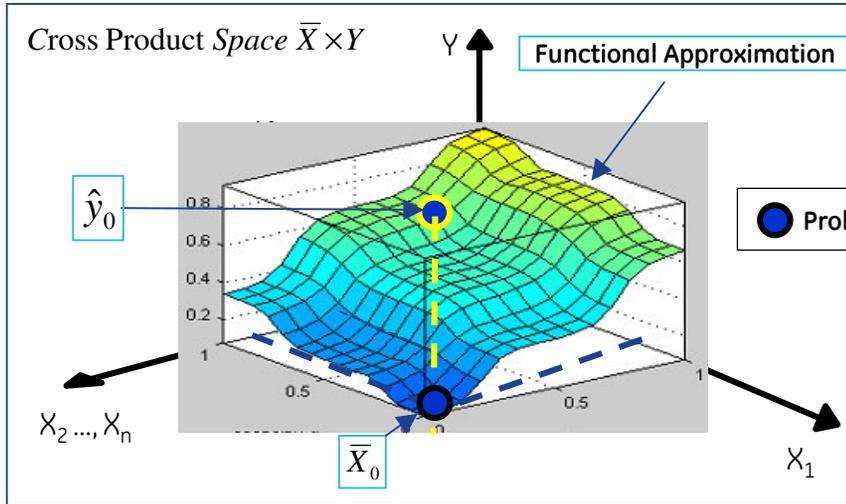
# Representation, Reasoning & Design Search

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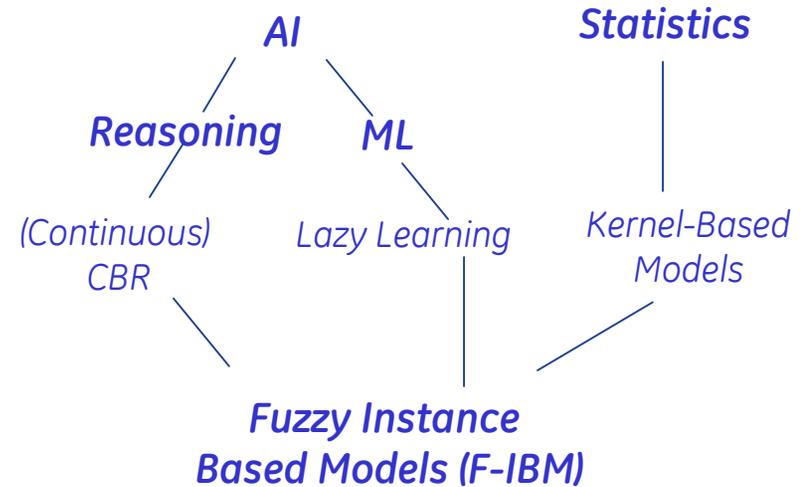
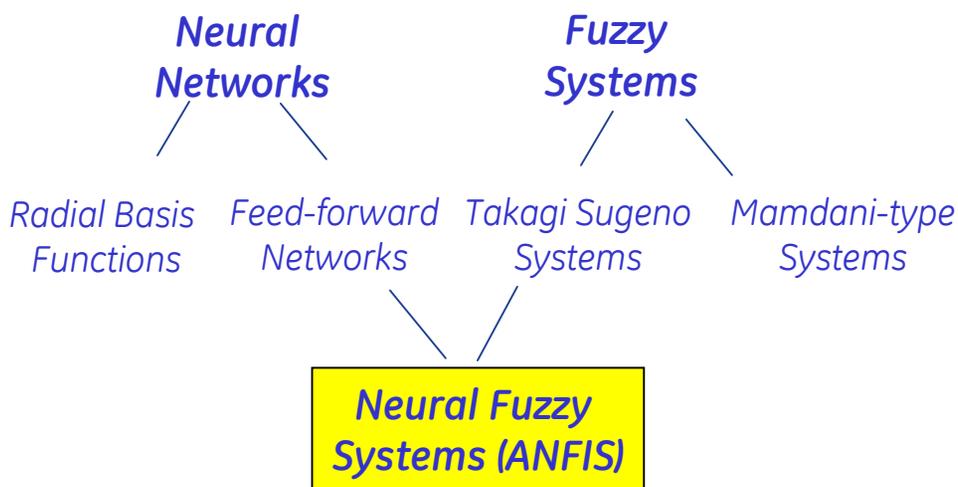
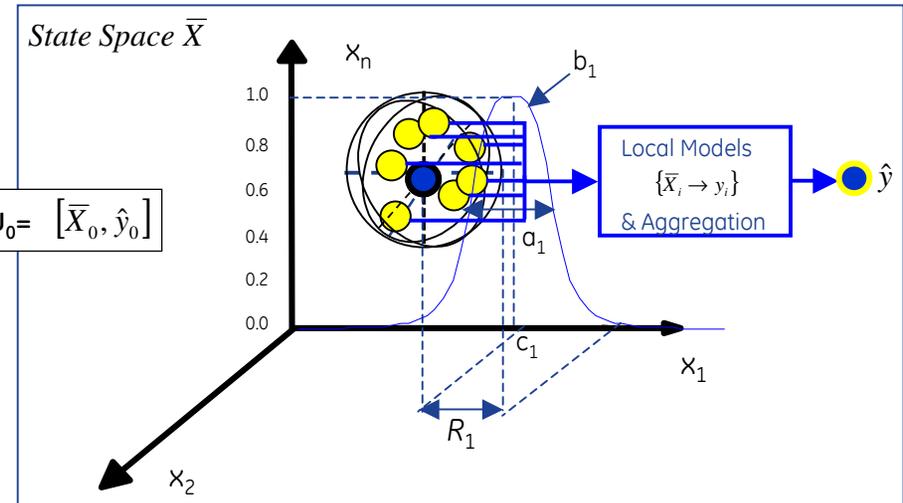
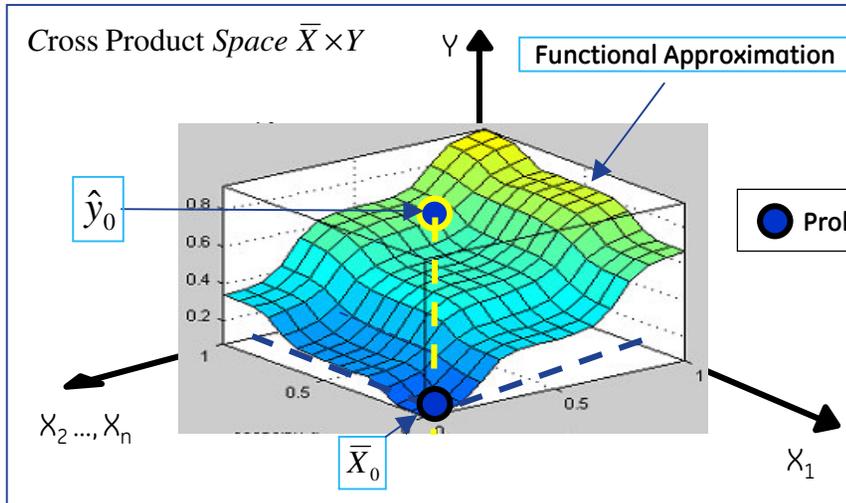
<b>Modeling Techniques</b>	<b>CLASSICAL:</b> <i>Linear Differential Equations</i>	<b>CI:</b> <i>Bayesian Belief Networks</i>	<b>CI:</b> <i>Neural Networks</i>	<b>CI:</b> <i>Fuzzy Systems TSK/ ANFIS</i>	<b>CI:</b> <i>Fuzzy Instance Based Reasoning</i>
<i>Model Structure</i>	Order	Topology	Topology	Rule Set	Attribute Space
<i>Model Parameters</i>	Coefficients	Prior Prob. Conditional Prob.	Biases Weights	Term sets Scaling Factors Coefficients	Attribute weights Similarity parameters
<i>Reasoning Mechanism</i>	Solve equations - Closed form - Approximation	Propagation	Propagation	Node evaluation & Propagation	Local Model evaluation & Output combination
<i>Design Search Method</i>	First principle Energy balance methods (Bond Graphs)	Manual EM EA ...	Manual EA Backpropagation Conjugate gradient,	Manual EA Backpropagation ... 	Manual EA ... 

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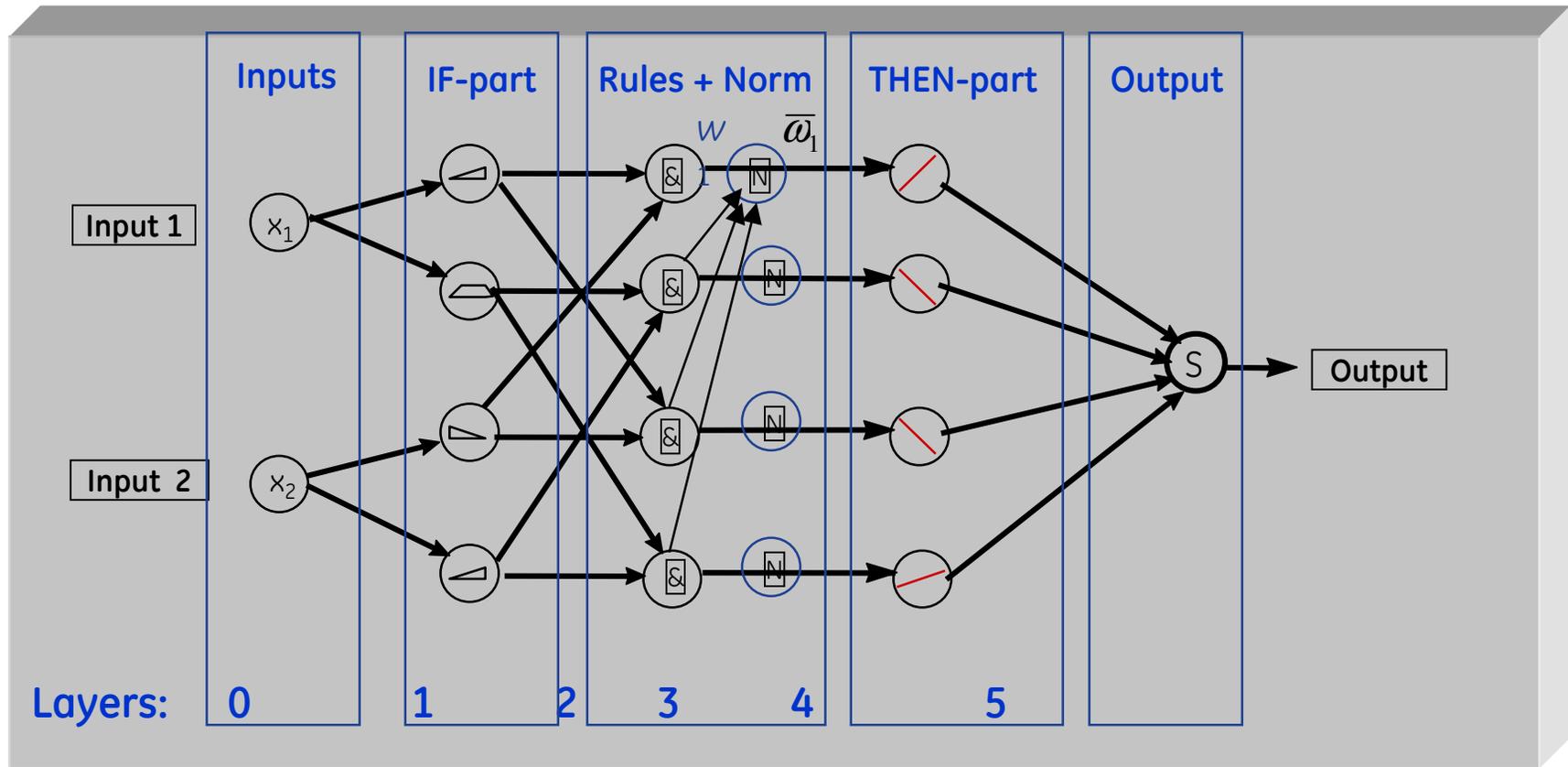
# Functional Approximation vs. Instance-Based



# Functional Approximation vs. Instance-Based



# ANFIS Network



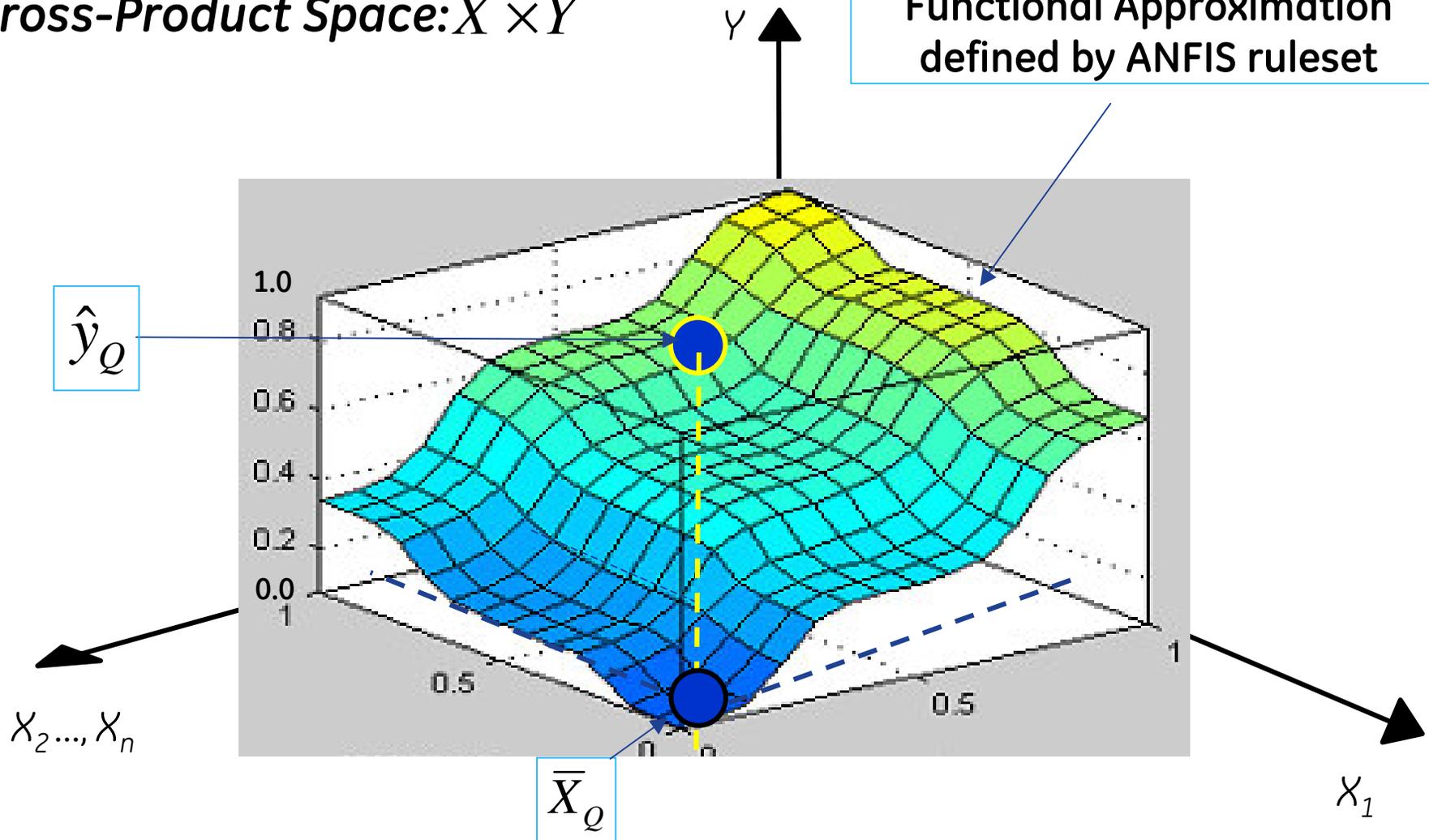
- $L_0$ : Inputs layer nodes: State variables
- $L_1$ : Values layer nodes: State variable Termsets, computing the membership value of inputs
- $L_2$ : Rules layer nodes: Fuzzy Rules, using product to compute rule matching factor  $w_i$
- $L_3$ : Normalization layer nodes: Each  $w_i$  is normalized (to add up to one) generating  $\bar{\omega}_i$
- $L_4$ : Function layer nodes: Linear regressions  $f_i$  are evaluated, generating rule outputs  $y_i$  that are weighted by normalized rule matching factors  $\bar{\omega}_i$
- $L_5$ : Output layer node: Sum of weighted outputs - (completing weighted average  $\omega_i$  outputs  $y_i$ )



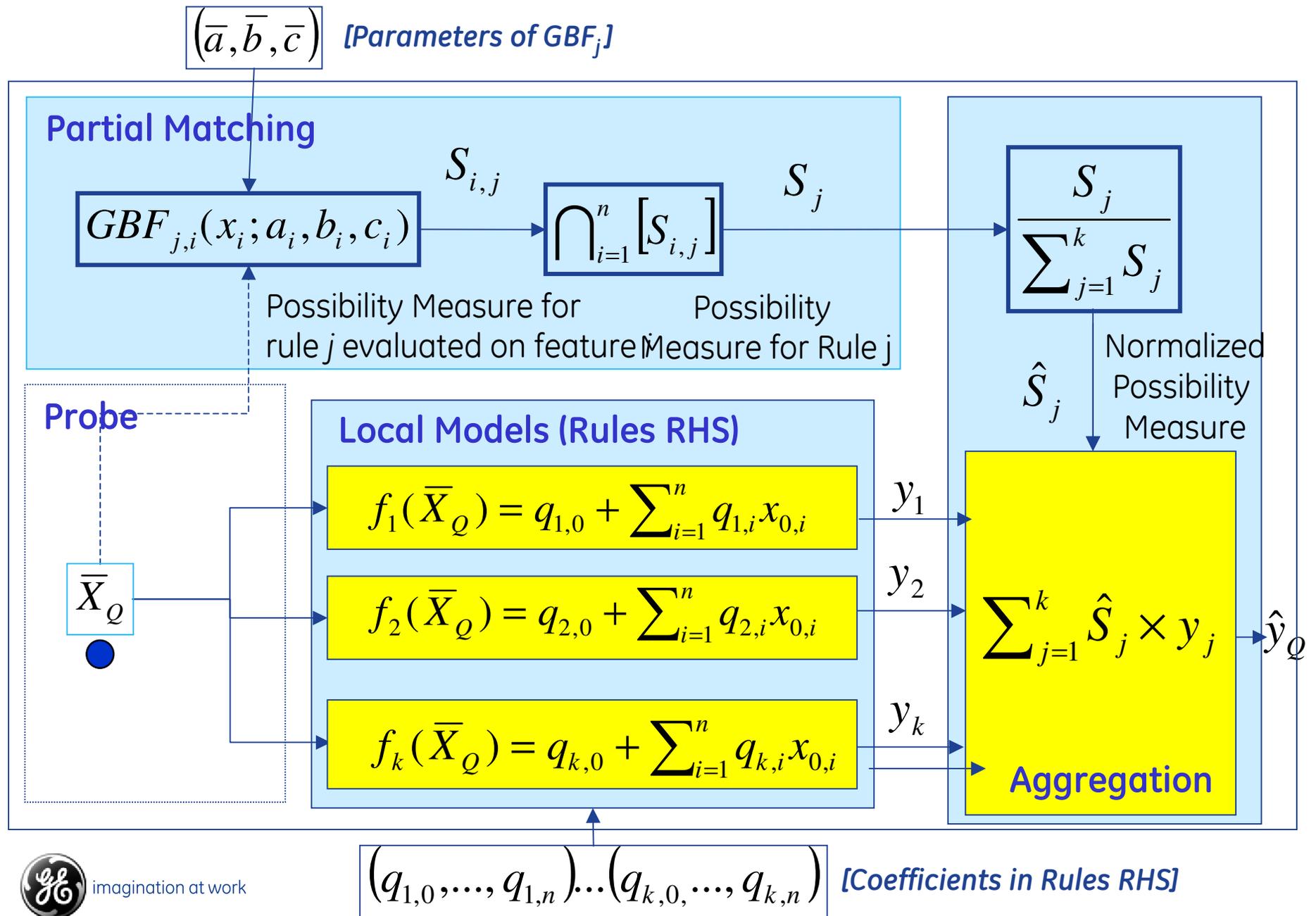
# ANFIS Reasoning: Geometrical Interpretation

Cross-Product Space:  $\bar{X} \times Y$

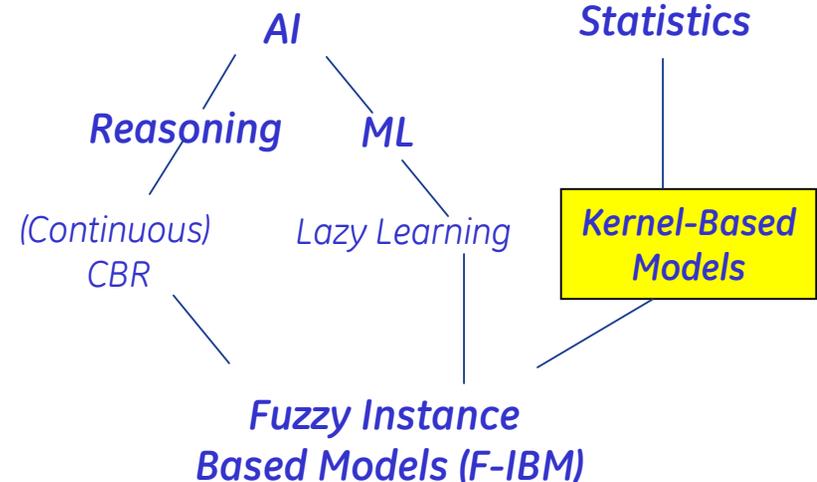
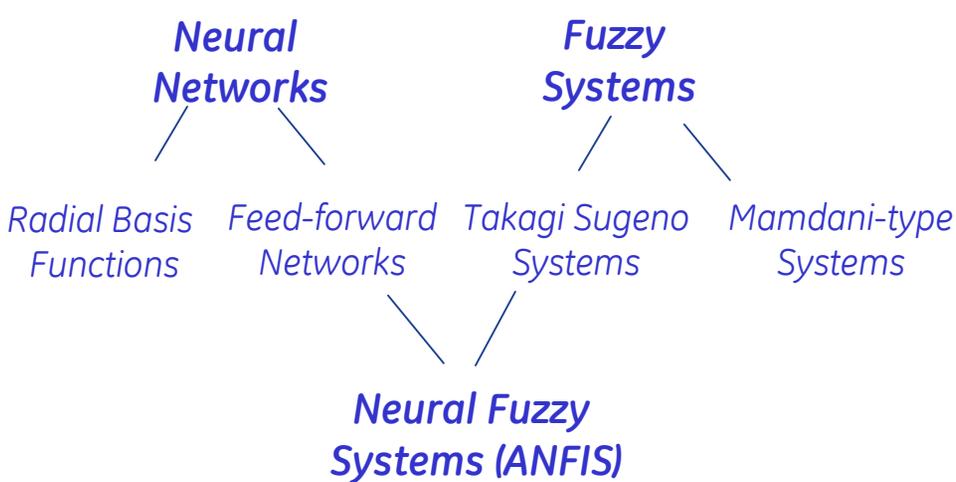
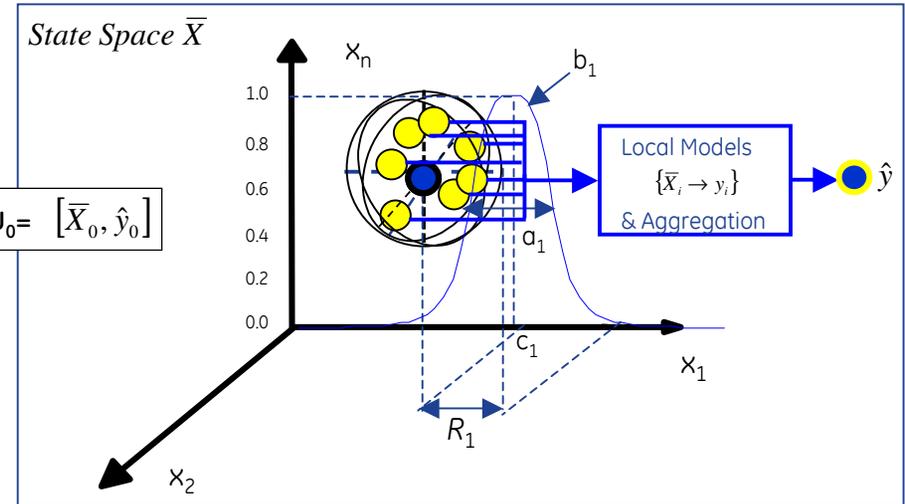
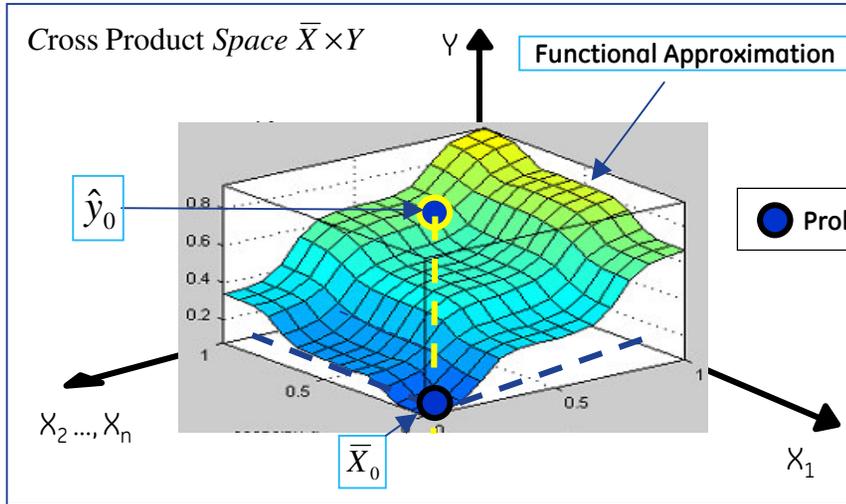
Functional Approximation  
defined by ANFIS ruleset



# ANFIS Reasoning: Algebraic Interpretation



# Functional Approximation vs. Instance-Based



To FIBM

# Kernel-based Models

## Classical Kernel-based Models

We have:

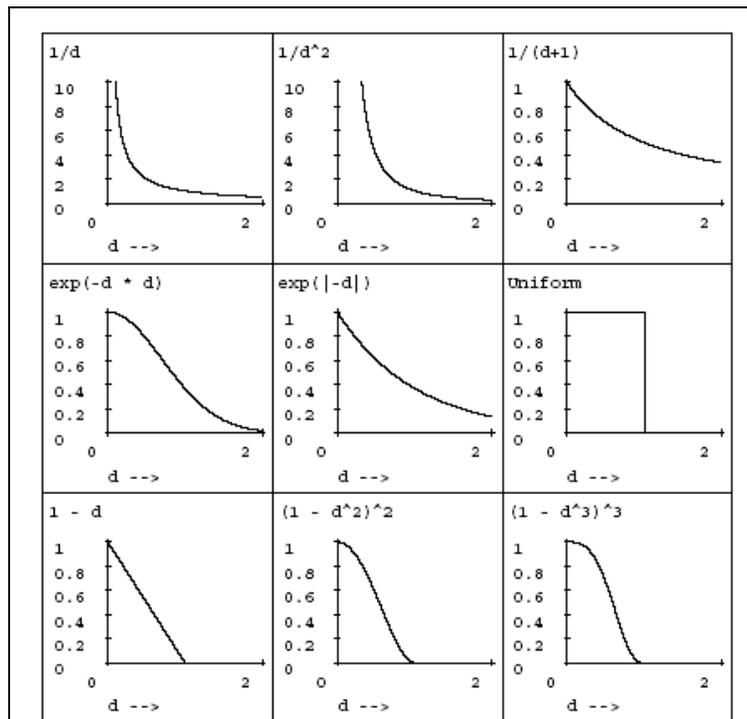
- a collection of points  $\{u_j\}$ :
- a Query  $Q$  defined in the  $\bar{X}$  space
- a Kernel function of the distance between each data point and the query, and a smoothing parameter  $h$

$$u_j = [\bar{X}_j; y_j] = [x_{1,j}, x_{2,j}, \dots, x_{n,j}; y_j] \quad \text{where } j = 1, \dots, k$$

$$Q = [\bar{X}_Q; \hat{y}_Q] = [x_{1,Q}, x_{2,Q}, \dots, x_{n,Q}; ?] \quad \text{where } |\bar{X}_Q| = |\bar{X}_j| = n$$

$$K\left(\frac{d(\bar{X}_j, \bar{X}_Q)}{h}\right)$$

### Examples of Kernel Functions $K$



### Examples of Distances $d$

(from Atkeson, Moore, Schaal, 1996)

- Unweighted Euclidean distance:

$$d_E(\mathbf{x}, \mathbf{q}) = \sqrt{\sum_j (\mathbf{x}_j - \mathbf{q}_j)^2} = \sqrt{(\mathbf{x} - \mathbf{q})^T (\mathbf{x} - \mathbf{q})} \quad (24)$$

- Diagonally weighted Euclidean distance:

$$d_m(\mathbf{x}, \mathbf{q}) = \sqrt{\sum_j (m_j (\mathbf{x}_j - \mathbf{q}_j))^2} = \sqrt{(\mathbf{x} - \mathbf{q})^T \mathbf{M}^T \mathbf{M} (\mathbf{x} - \mathbf{q})} = d_E(\mathbf{M}\mathbf{x}, \mathbf{M}\mathbf{q}) \quad (25)$$

where  $m_j$  is the feature scaling factor for the  $j$ th dimension and  $\mathbf{M}$  is a diagonal matrix with  $\mathbf{M}_{jj} = m_j$ .

- Fully weighted Euclidean distance:

$$d_M(\mathbf{x}, \mathbf{q}) = \sqrt{(\mathbf{x} - \mathbf{q})^T \mathbf{M}^T \mathbf{M} (\mathbf{x} - \mathbf{q})} = d_E(\mathbf{M}\mathbf{x}, \mathbf{M}\mathbf{q}) \quad (26)$$

where  $\mathbf{M}$  is no longer diagonal but can be arbitrary. This is also known as the Mahalanobis distance (Tou and Gonzalez, 1974; Weisberg, 1985).

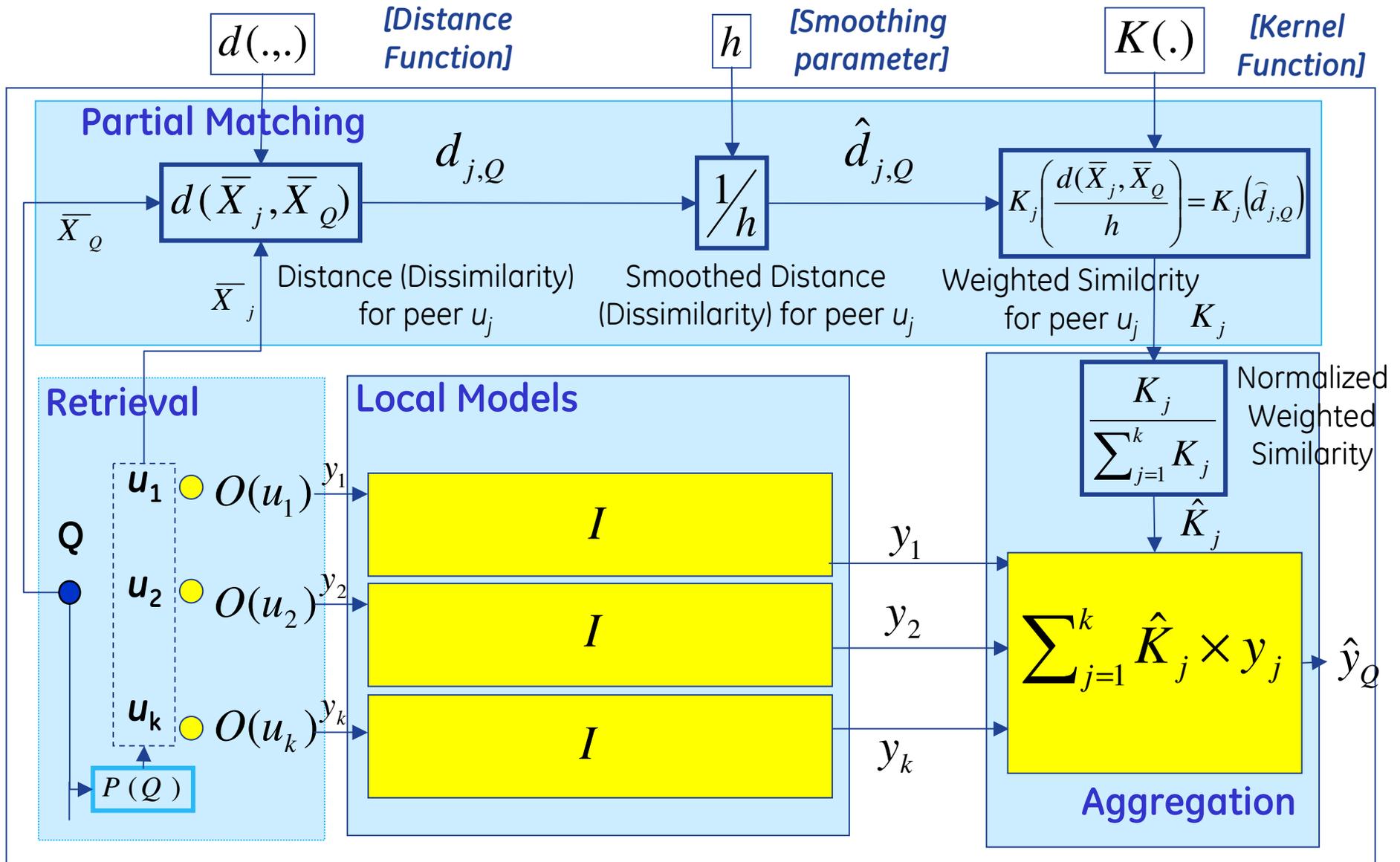
- Unweighted  $L_p$  norm (Minkowski metric):

$$d_p(\mathbf{x}, \mathbf{q}) = \left( \sum_i |\mathbf{x}_i - \mathbf{q}_i|^p \right)^{\frac{1}{p}} \quad (7)$$

- Diagonally weighted and fully weighted  $L_p$  norm: The weighted  $L_p$  norm is  $d_p(\mathbf{M}\mathbf{x}, \mathbf{M}\mathbf{q})$ .



# Kernel-based Models: Nadaraya-Watson Estim.



# Kernel-based Models: Weighted Regression

## Kernel-based Regressions

### Data Weighting Process:

- Use the Kernel function (evaluated at each point  $u_j$ ) as a weight
- Create a diagonal  $[k \times k]$  matrix  $\mathbf{W}$  with diagonal elements  $W_{jj} = w_j$  and zeros elsewhere
- Create a  $[k \times n]$  matrix  $\mathbf{X}$  with the original state data. The  $i^{\text{th}}$  row of  $\mathbf{X}$  contains the  $n$  coordinates of the  $i^{\text{th}}$  point, i.e.,  $\bar{\mathbf{X}}_i$
- Create a  $[k \times 1]$  vector  $\mathbf{Y}$  with the original output data. The  $i^{\text{th}}$  row of  $\mathbf{Y}$  contains the value of  $y_i$
- Weigh matrix  $\mathbf{X}$  and vector  $\mathbf{Y}$  using the weights  $\mathbf{W}$ :

$$w_j = \sqrt{K\left(\frac{d(\bar{\mathbf{X}}_j, \bar{\mathbf{X}}_Q)}{h}\right)}$$

$$\mathbf{Z} = \mathbf{W}\mathbf{X} \text{ and } \mathbf{V} = \mathbf{W}\mathbf{Y}$$

$$\mathbf{Z} \text{ is } [k \times n] \text{ and } \mathbf{V} \text{ is } [k \times 1]$$

- We want to solve the equation:

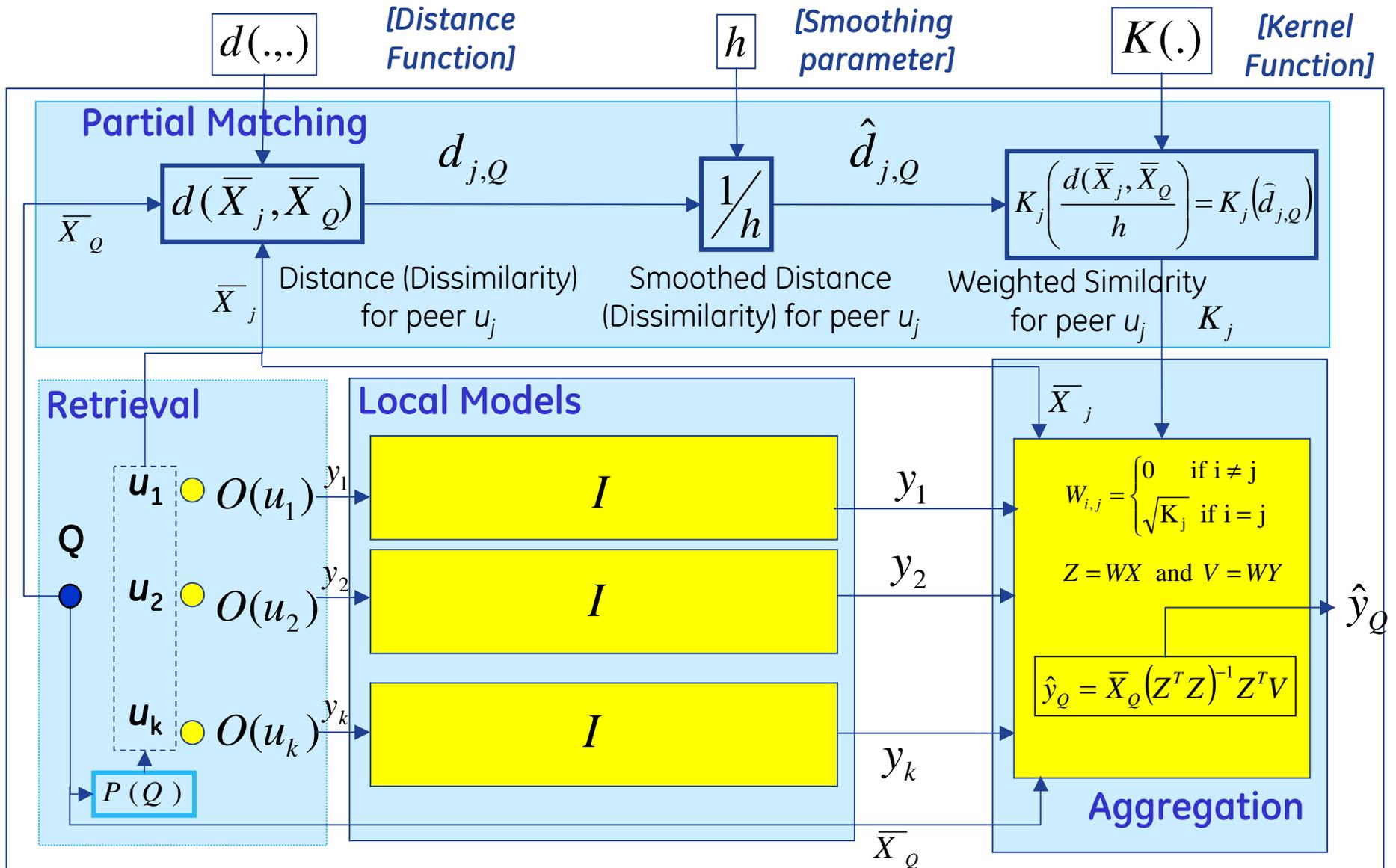
$$\hat{y}(Q) = \bar{\mathbf{X}}_Q (\mathbf{Z}^T \mathbf{Z})^{-1} \mathbf{Z}^T \mathbf{V}$$

which is predicated on having a non-singular  $[n \times n]$  matrix:  $(\mathbf{Z}^T \mathbf{Z})^{-1}$

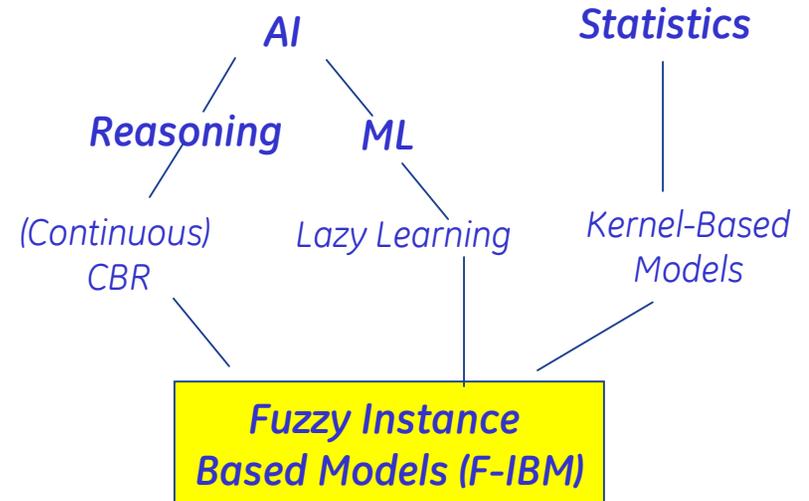
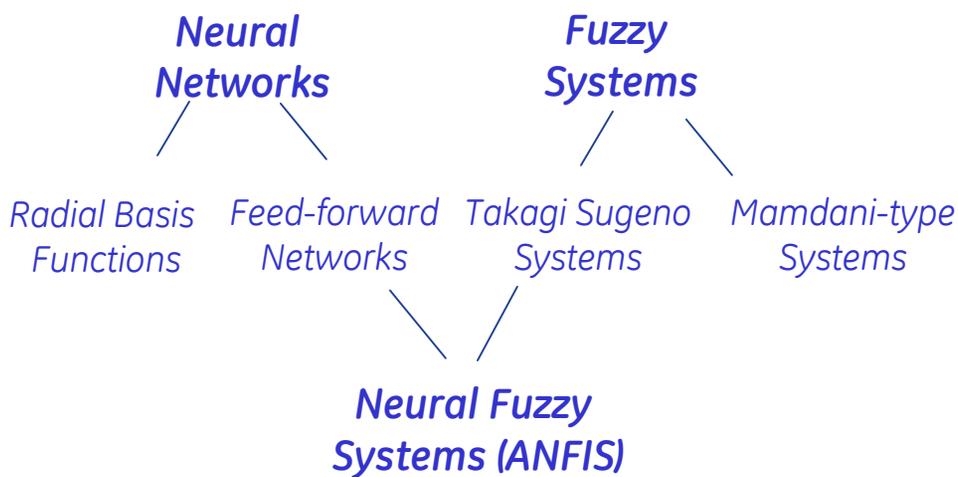
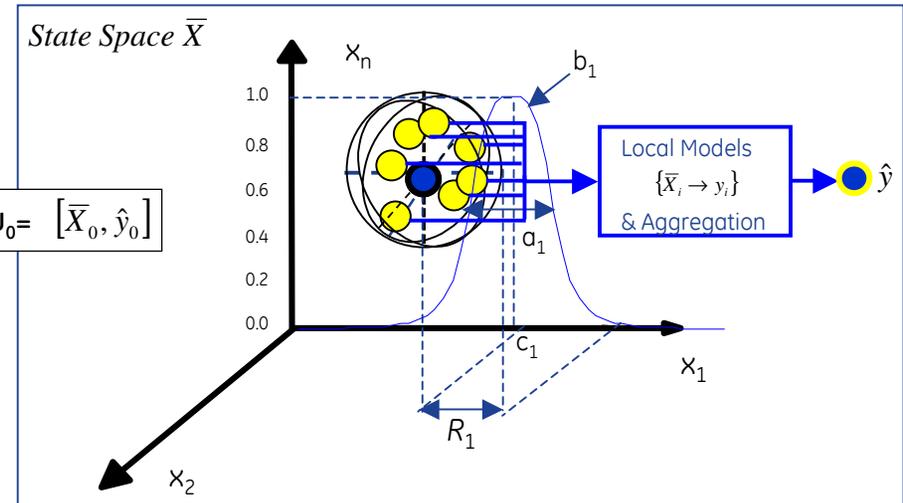
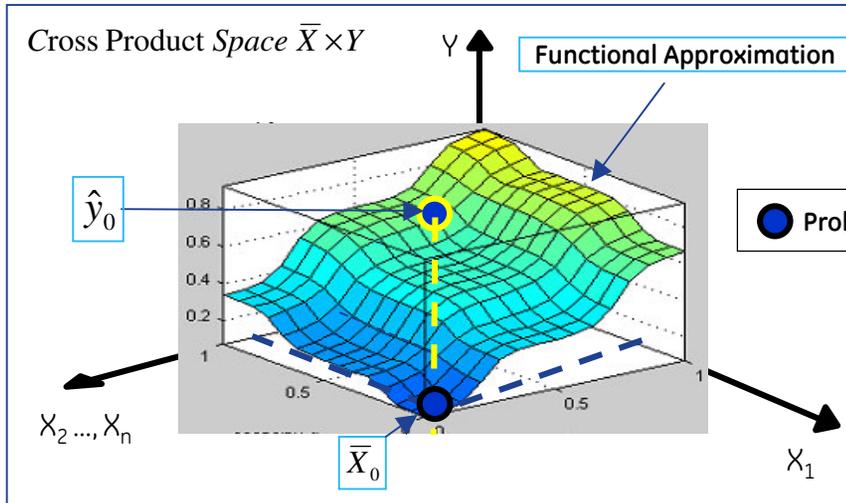
- When the matrix  $(\mathbf{Z}^T \mathbf{Z})^{-1}$  is singular we can resolve the issue using ridge regressions



# Kernel-based Models: Weighted Regression



# Functional Approximation vs. Instance-Based



# 4. Fuzzy Instance Based Model (F-IBM)

- Retrieval
- Similarity Evaluation
- Creation of Local Models
- Outputs Aggregation
- Evolutionary Search for Designing a F-IBM

# Fuzzy Instance Based Models (F-IBM's)

## Comparison with Case Based Reasoning

- IBM's rely on a collection of previously experienced data that can be store in their raw representation
- Unlike Case-based Models (CBM's), IBM's **do not need** to have data refined, abstracted and **organized as cases**
- Like CBM's, IBM's are based on analogical reasoning, as they rely upon finding previous instances of **similar** objects (or points) and use them to create an ensemble of local models

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- Unlike Case-based Models (CBM's), IBM's *do not need* to have data refined, abstracted and *organized as cases*
- Like CBM's, IBM's are based on analogical reasoning, as they rely upon finding previous instances of *similar* objects (or points) and use them to create an ensemble of local models

## Similarity Measure

- The definition of **similarity** plays a **critical** role in IBM's performance
- Similarity will be a **dynamic** concept and will change over time. Therefore, it is important to apply **learning** methodologies **to define it and adapt it.**
- Furthermore, the concept of similarity is not crisply defined, creating the need to allow for some degree of **vagueness** in its evaluation

# Fuzzy Instance Based Models (F-IBM's)

## Comparison with Case Based Reasoning

- IBM's rely on a collection of previously experienced data that can be store in their raw representation
- Unlike Case-based Models (CBM's), IBM's *do not need* to have data refined, abstracted and *organized as cases*
- Like CBM's, IBM's are based on analogical reasoning, as they rely upon finding previous instances of *similar* objects (or points) and use them to create an ensemble of local models

## Similarity Measure

- The definition of **similarity** plays a **critical** role in IBM's performance
- Similarity will be a **dynamic** concept and will change over time. Therefore, it is important to apply **learning** methodologies **to define it and adapt it.**
- Furthermore, the concept of similarity is not crisply defined, creating the need to allow for some degree of **vagueness** in its evaluation

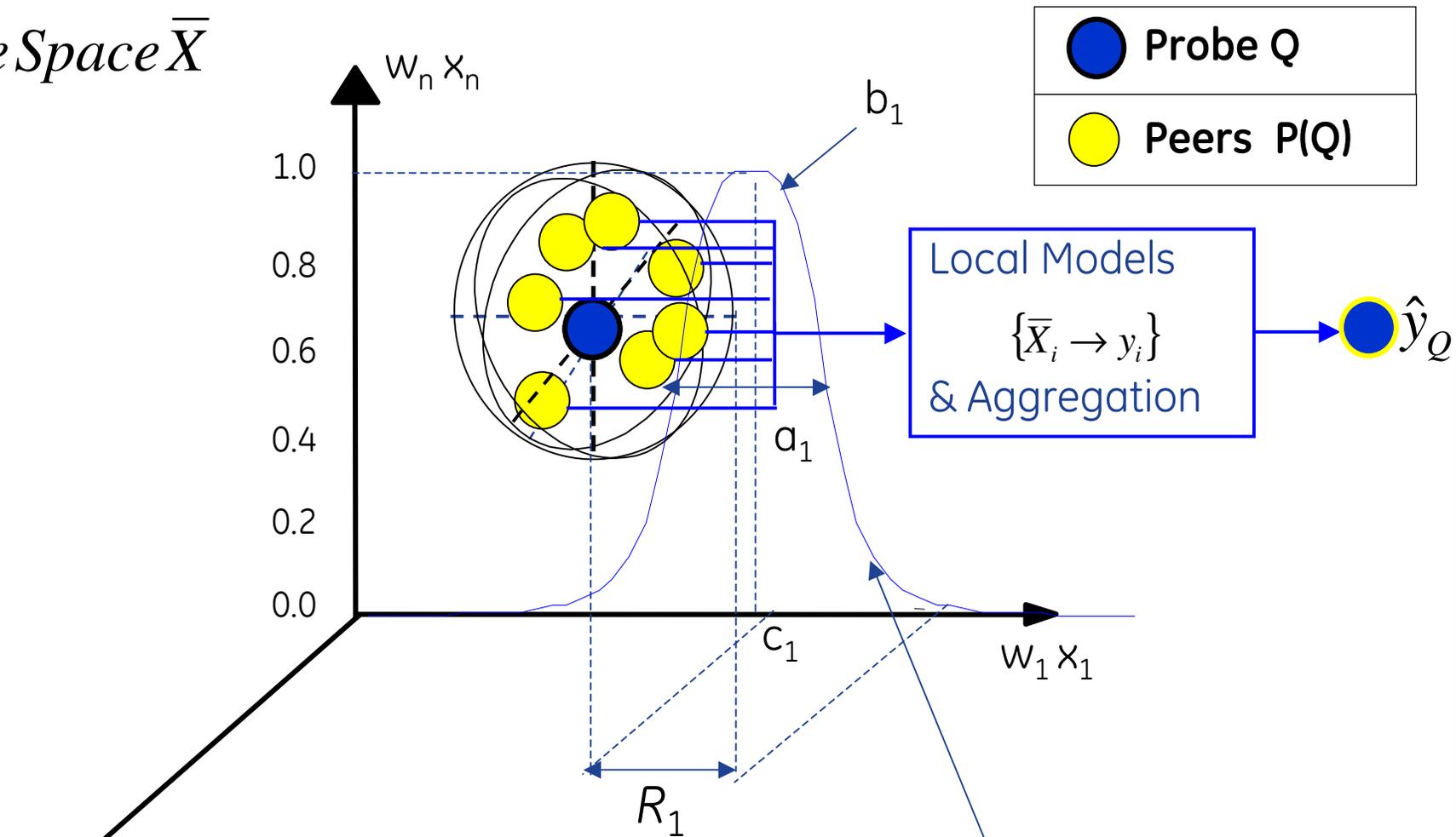
## Solution:

- By using a **wrapper** approach, we **evolve** the **design of the similarity** function and the **design of the attribute space** in which the similarity is to be evaluated.



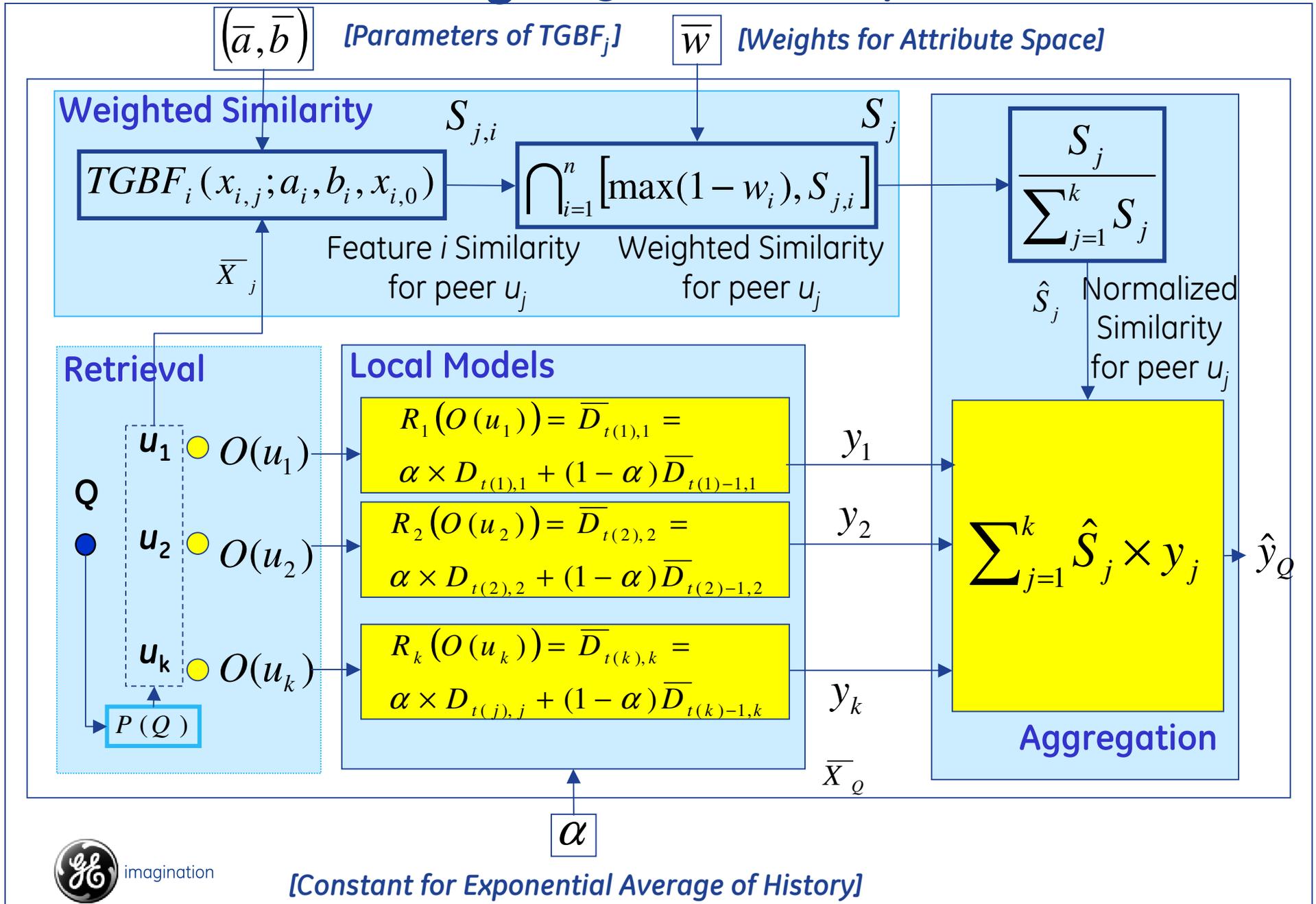
# F-IBM Reasoning: Geometrical Interpretation

State Space  $\bar{X}$



$$TGBF_i(x_i; a_i, b_i, c_i) = \begin{cases} \frac{1}{1 + \left| \frac{x_i - c_i}{a_i} \right|^{2b_i}} & \text{if } GBF > 10^{-5} \\ 0 & \text{otherwise} \end{cases}$$

# F-IBM Reasoning: Algebraic Interpretation



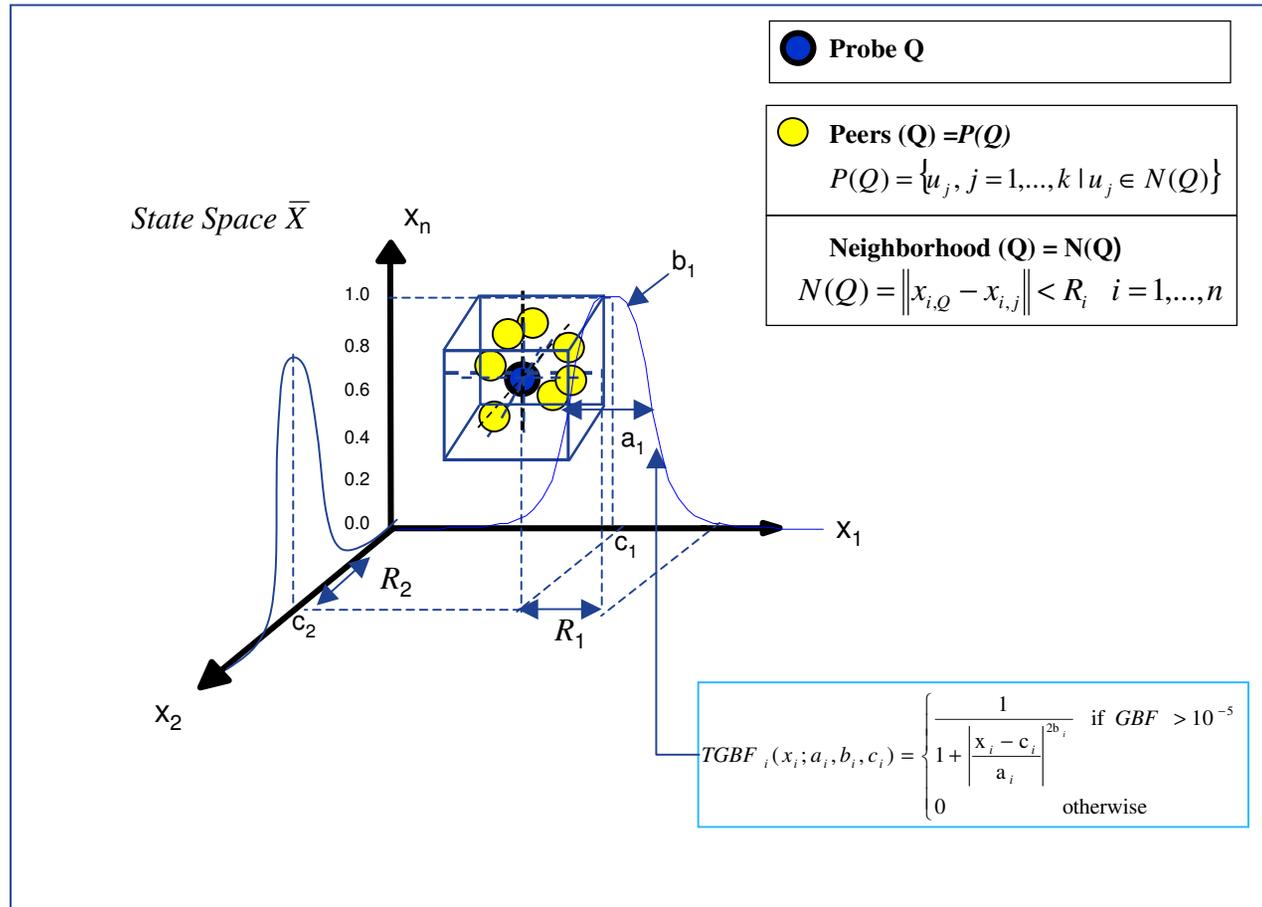
# Fuzzy Instance Based Models (F-IBM's)

We address this design issues by evolving the design of a similarity function in conjunction with the design of the attribute space in which similarity is evaluated. Specifically we us the following four steps:

- 1) **Retrieval** of similar instances from the Data Base
- 2) **Evaluation of similarity measure** between the probe and the retrieved instances
- 3) **Creation of local models** using the most similar instances
- 4) **Outputs Aggregation** (weighted by their similarities)

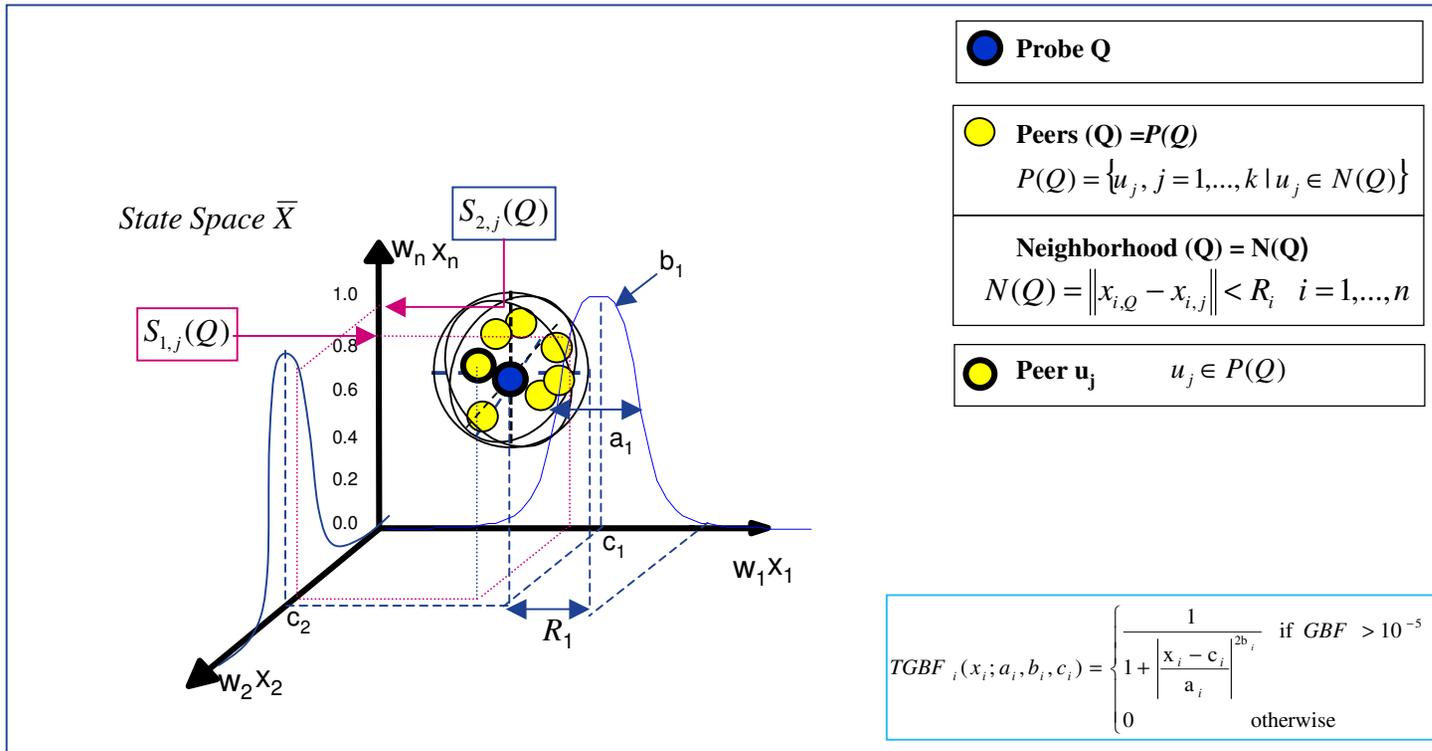
Let us explain the four steps

# (1) Retrieval



Representation	Feature Space	History
<b>Probe</b> $Q = [\bar{X}_Q; O(Q)]$	$\bar{X}_Q = [x_{1,Q}, \dots, x_{n,Q}]$	<b>History of Probe</b> $O(Q) = [D_{1,Q}, \dots, D_{t(Q),Q}]$
<b>Peer</b> $u_j = [\bar{X}_j; O(u_j)]$	$\bar{X}_j = [x_{1,j}, \dots, x_{n,j}]$	<b>History of Peer</b> $O(u_j) = [D_{1,j}, D_{2,j}, \dots, D_{t(j),j}]$

# (2) Similarity Evaluation



**$S_j$  = Similarity between Probe Q and Peer  $u_j$**

$$S_j = \text{Min}_{i=1}^n \{S_{i,j}\} = \text{Min}_{i=1}^n TGBF(x_{i,j}; a_i, b_i, x_{i,Q})$$

**$S_j$  = Weighted Similarity between Probe Q and Peer  $u_j$**

$$S_j = \text{Min}_{i=1}^n \{ \text{Max} [(1 - w_i), S_{i,j}] \} = \text{Min}_{i=1}^n \{ \text{Max} [(1 - w_i), TGBF_i(x_i; a_i, b_i, x_{i,Q})] \}$$



# (3) Creation of Local Models

## Local Models

Rather than using a pre-constructed model, as in ANFIS or other functional approximators, we use local models, as in memory-based approaches, kernel-based regressions, and lazy-learning.

In this example, each retrieved object  $u_j$  has an associated time-series:

$$O(u_j) = [D_{1,j}, D_{2,j}, \dots, D_{t(j),j}]$$

One of the simplest local models that we can create is the **exponential average**, that will “discount” the oldest data, using a forgetting factor  $\alpha$ .

The peer  $u_j$  of the probe will produce an output  $y_j$  representing the prediction for the next point in the time-series:

$$\begin{aligned} y_j &= D_{t(j)+1,j} \\ &= \bar{D}_{t(j),j} = \alpha \times D_{t(j),j} + (1 - \alpha) \times \bar{D}_{t(j)-1,j} \quad [\text{where } \bar{D}_{1,j} = D_{1,j}] \\ &= (1 - \alpha)^{k(j)-1} D_{1,j} + \sum_{i=2}^{t(j)} (1 - \alpha)^{t(j)-i} \times \alpha \times D_{i,j} \end{aligned}$$



## (4) Outputs Aggregation

### Outputs Aggregation *(weighted by their similarities)*

We need to combine the individual predictions  $\{D_{t(j)+1,j}\}$  ( $j=1,\dots, k$ ) obtained from the peers  $u_j(Q)$  to generate the next prediction  $D_{Next,Q}$  for the probe  $Q$

To this end, we compute the weighted average of the peers' individual predictions using their normalized similarity to the probe as a weight:

$$\hat{y}_Q = D_{Next,Q} = \frac{\sum_{j=1}^k S_j \times D_{t(j)+1,j}}{\sum_{j=1}^k S_j} = \frac{\sum_{j=1}^k S_j \times y_j}{\sum_{j=1}^k S_j}$$

If we define the normalized weights as:  $\hat{S}_j = \frac{S_j}{\sum_{j=1}^k S_j}$

then the above expression can be rewritten as:

$$\hat{y}_Q = \sum_{j=1}^k \hat{S}_j \times y_j = \langle \hat{S}, Y \rangle$$

## (4) Outputs Aggregation (cont.)

**Outputs Aggregation** (weighted by their similarities)

$$\hat{y}_Q = D_{Next,Q} = \frac{\sum_{j=1}^k S_j \times y_j}{\sum_{j=1}^k S_j}$$

Note that this expression (a convex sum of local models outputs using the similarities as weights) is similar to the structure of the **Nadaraya-Watson** [1964] estimator for non-parametric regressions using locally weighted averages – where the weights are the values of a kernel function  $K$ :

$$\hat{y}_Q = \frac{\sum_{j=1}^k K(x - x_j) \times y_j}{\sum_{j=1}^k K(x - x_j)}$$

From this analogy, we can see a structural similarity between the Similarity measures  $S_j$  used by the Instance-based method and the Kernel functions  $K$  evaluated on the distance between the probe and each point, i.e.:

$$S_j \approx K(x - x_j)$$

# Evolutionary Search

## EA to Search in Design Space

The EA is composed of a population of individuals (“chromosomes”), each of which contains a vector of elements representing distinct tuneable parameters within the FIM configuration.

The EA used two types of mutation operators (Gaussian and uniform), and no crossover. Its population (with 100 individuals) was evolved over 200 generations

Each chromosome defines an instance of the attribute space used by the associated model by specifying a vector of weights  $[w_1, w_2, \dots, w_n]$ .

# Evolutionary Search

## EA to Search in Design Space

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Each chromosome defines an instance of the attribute space used by the associated model by specifying a vector of weights  $[w_1, w_2, \dots, w_n]$ .

If  $w_i \in \{0,1\}$  we perform *attribute selection*, i.e., we select a crisp subset from the universe of potential attributes.

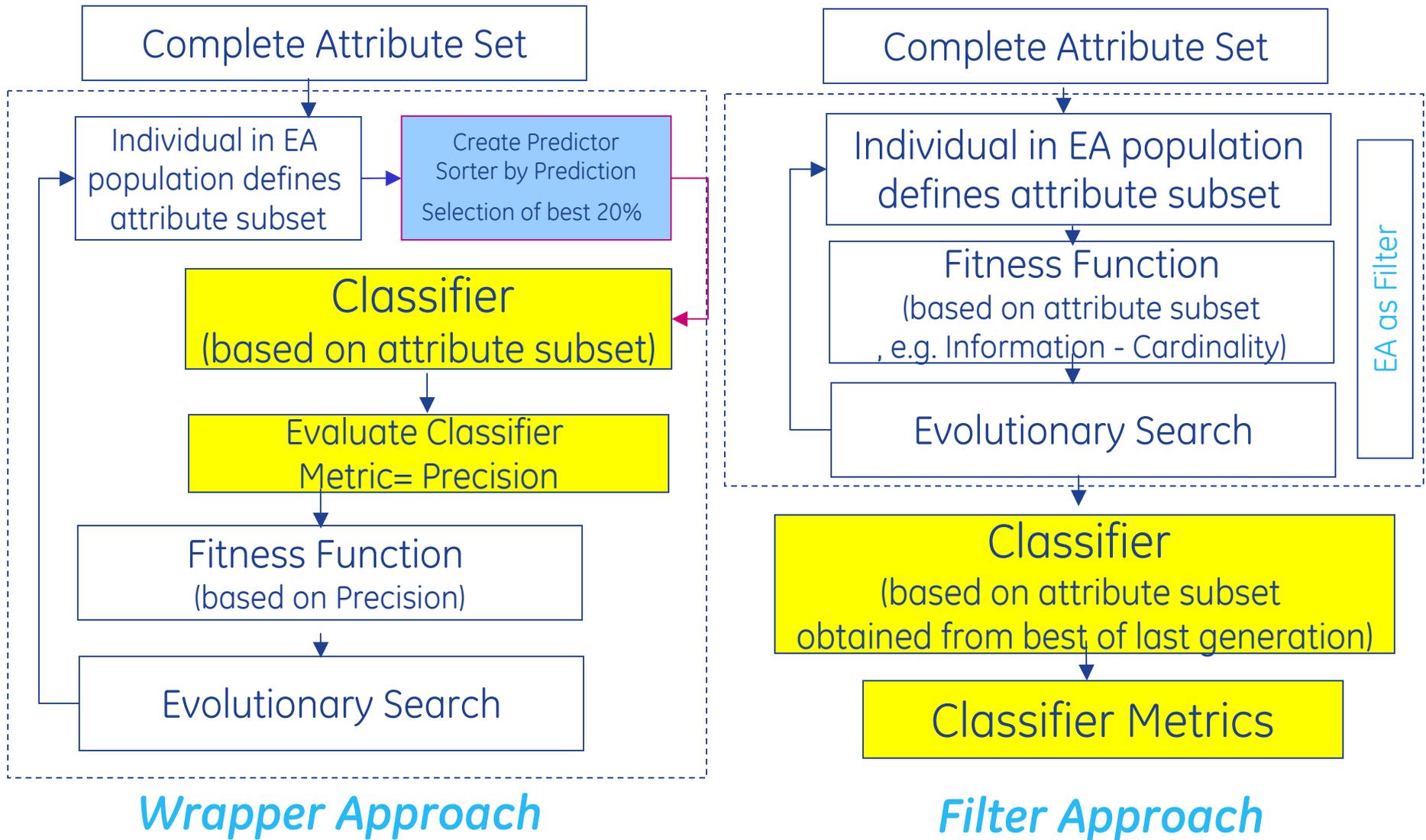
If  $w_i \in [0,1]$  we perform *attribute weighting*, i.e., we define a fuzzy subset from the universe of potential attributes

Chromosome representation:

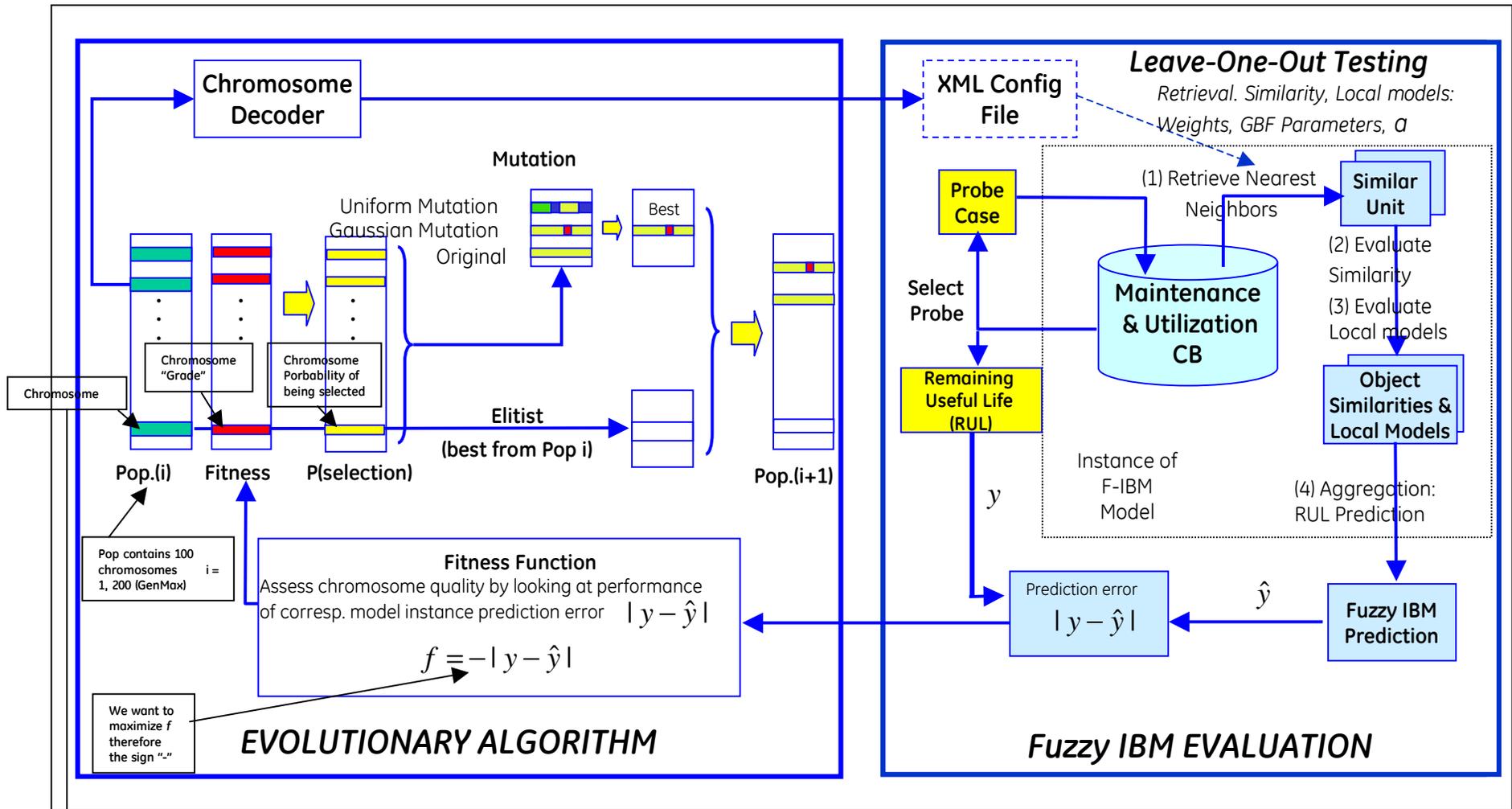
$$[w_1 \ w_2 \ \dots \ w_n] [(a_1, b_1), (a_2, b_2), \dots, (a_n, b_n)] [\alpha]$$



# Wrapper and Filter Approaches



# Evolutionary Search for Designing A Fuzzy IBM (Predictor) using a Wrapper Approach



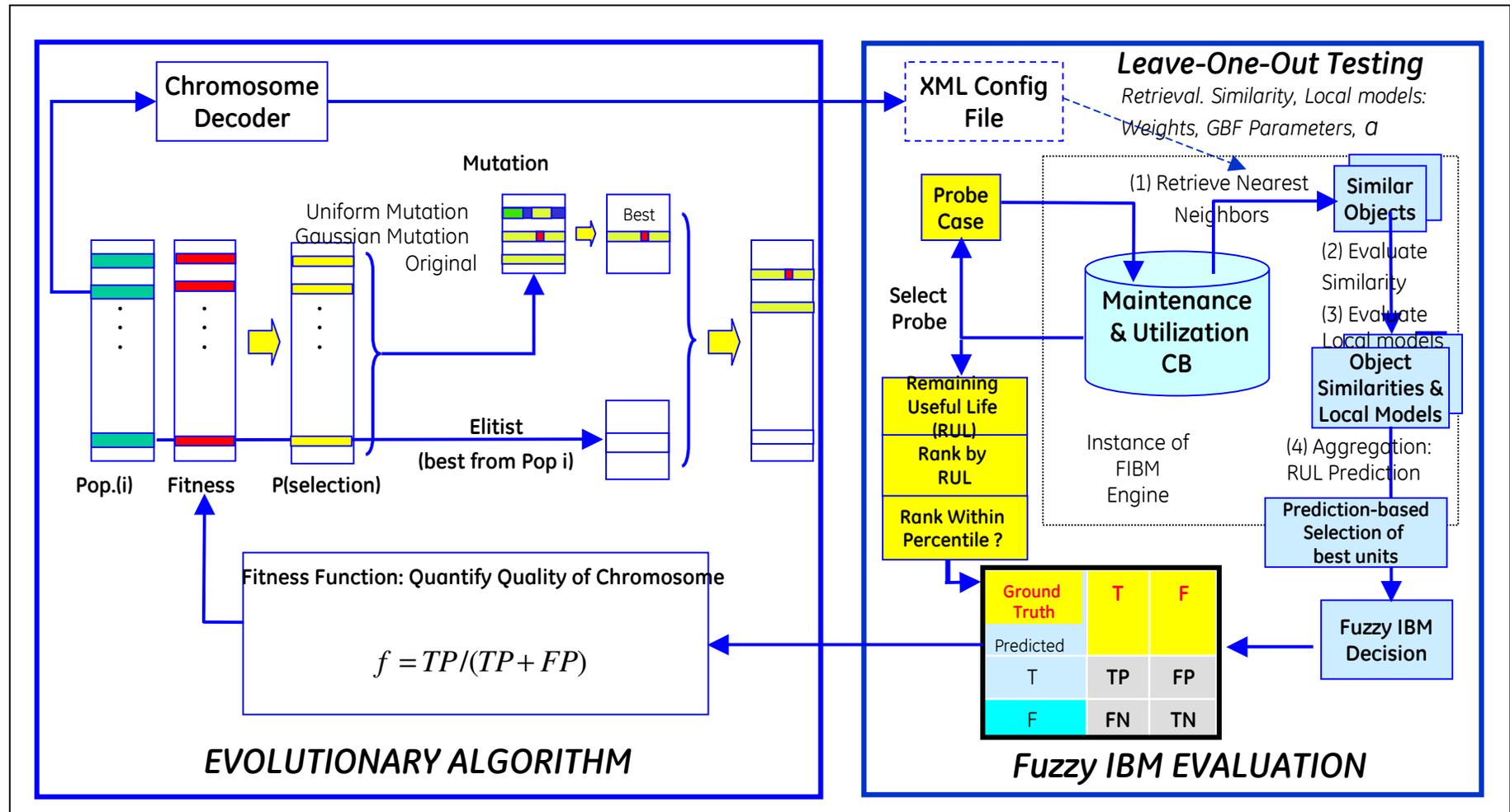
Chromosome:

$$[w_1 \ w_2 \ \dots \ w_n] [(a_1, b_1), (a_2, b_2), \dots, (a_n, b_n)] [\alpha]$$



$w_1 = 0 \rightarrow X_1$  IS NOT selected & we do not care about  $(a_1, b_1)$  - since we do not use  $X_1$   
 $w_1 = 1 \rightarrow X_1$  IS selected &  $(a_1, b_1)$  define how tolerant (high  $a_1$ , low  $b_1$ ) or strict (low  $a_1$ , high  $b_1$ ) we want to be when evaluating similarity along  $x_1$

# Evolutionary Search for Designing A Fuzzy IBM (Classifier) using a Wrapper Approach



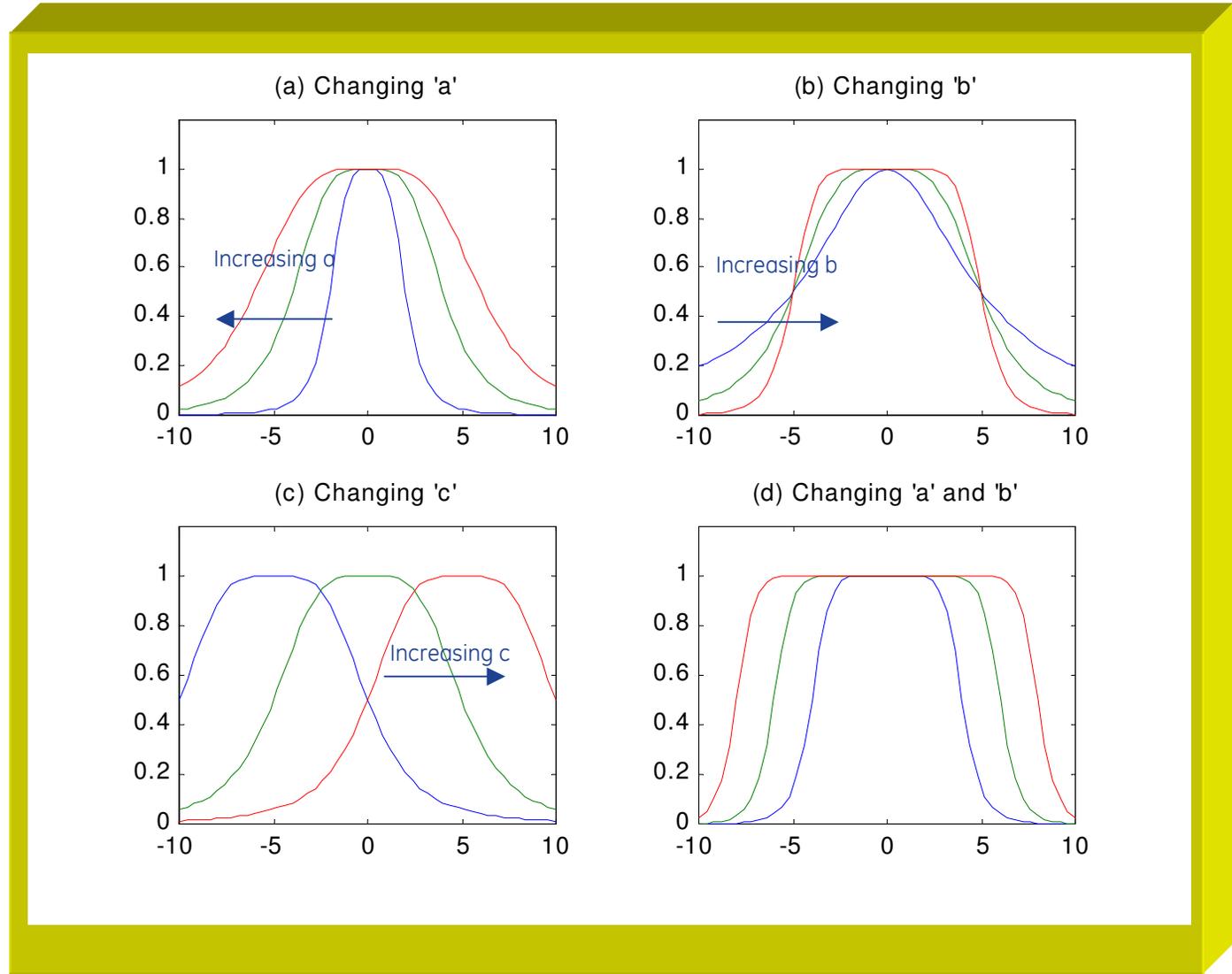
Chromosome:  $[w_1 w_2 \dots w_n] [(a_1, b_1), (a_2, b_2), \dots, (a_n, b_n)] [\alpha]$



To Example

# Effect of Changing Parameters {a,b,c}

$$\mu_A(x) = \frac{1}{1 + \left| \frac{x - c_i}{a_i} \right|^{2b}}$$



Chromosome  $\Rightarrow [w_1 \ w_2 \ \dots \ w_n] [(a_1, b_1), (a_2, b_2), \dots, (a_n, b_n)] [\alpha]$

# 5. Case Study: Prediction of Best Units for Asset Selection

- Asset Selection for Mission Reliability: A locomotive example
- Data Collection, Baselines, and Experiments
- Peer Learning Methodology
- Results & Conclusions

# Asset Selection Outline

- Problem Description
- Data Collection and Experiments Set-Up
- Proposed Peer-Learning Methodology
- Results
- Conclusions

# Asset Selection Outline



- **Problem Description**

- *Mission Reliability*
- *The Selection Problem*

- Data Collection and Experiments Set-Up

- Proposed Peer-Learning Methodology

- Results

- Conclusions



# The Premise

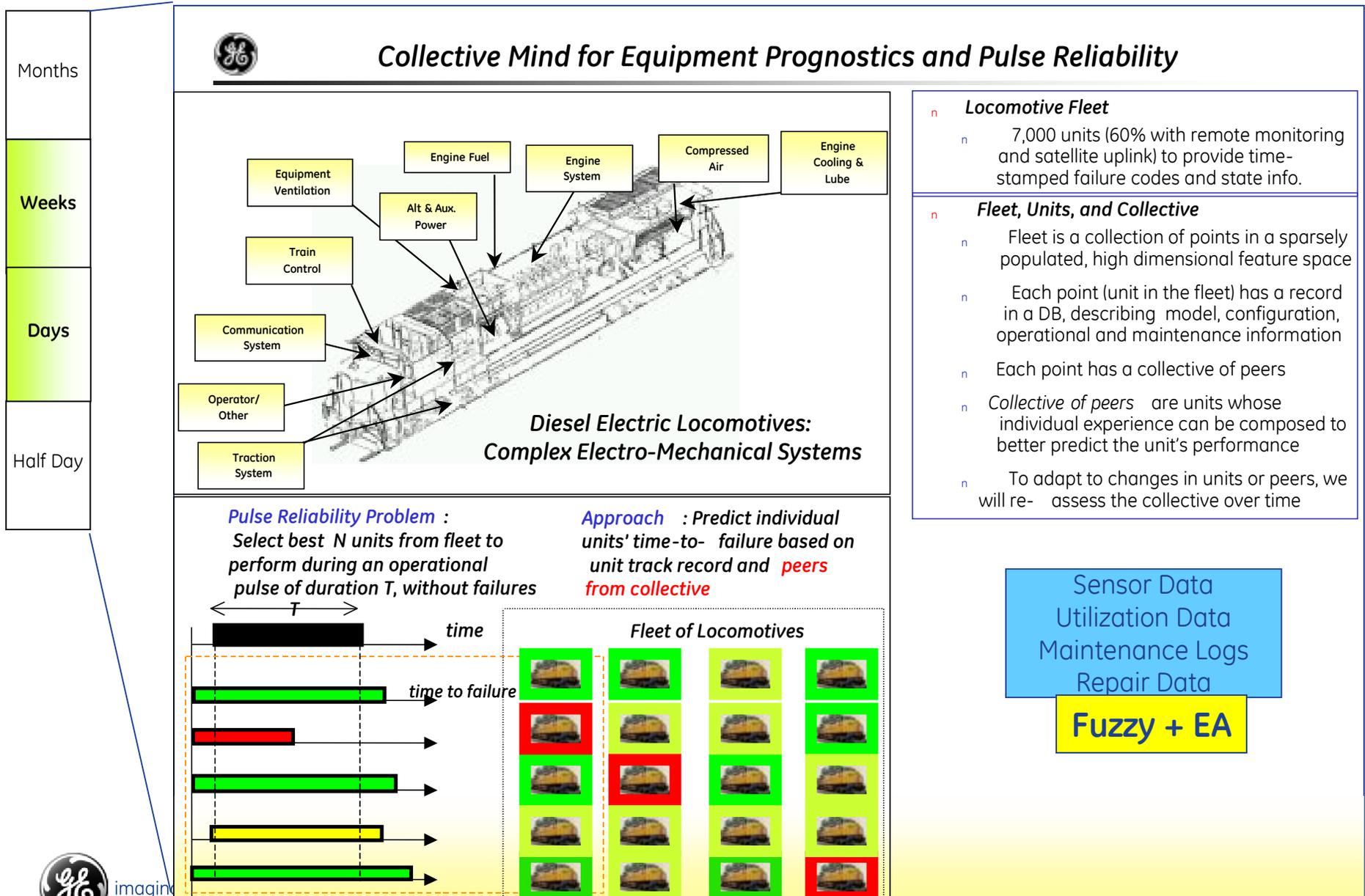
**New learning approaches** can address early phases of new platform deployment with limited operational and sensor data.

-Learning using **existing utilization and maintenance history** improves our ability to select the best units for a mission, leading to better utilization of existing assets.

-**Learning from peers** is a robust approach to rapid learning from limited data.

-**Evolutionary Learning** provides a comprehensive framework for automating the design and maintenance of a classifier used for selection of the best assets.

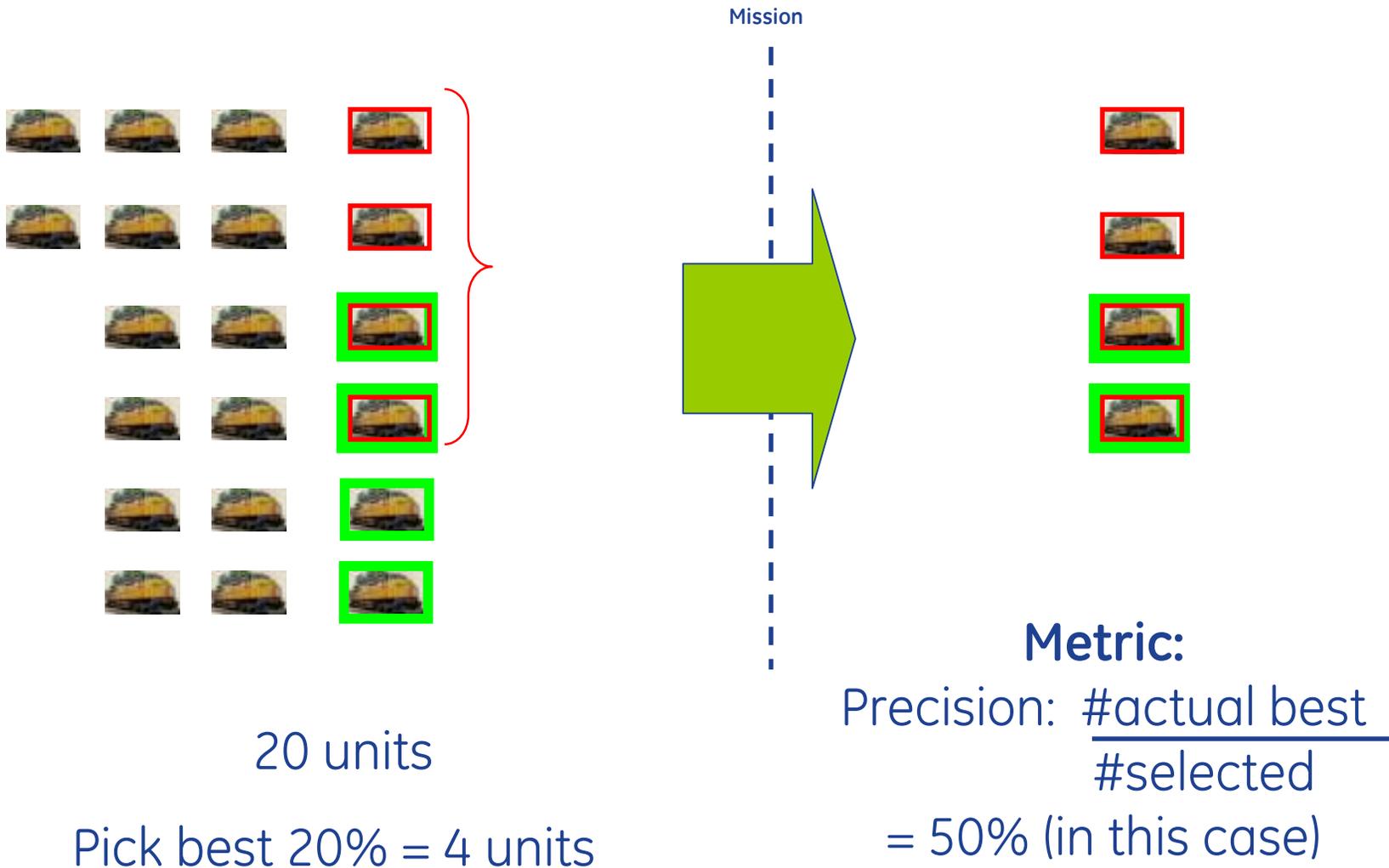
# Asset Selection Based on Predicted Life



- n **Locomotive Fleet**
  - n 7,000 units (60% with remote monitoring and satellite uplink) to provide time-stamped failure codes and state info.
- n **Fleet, Units, and Collective**
  - n Fleet is a collection of points in a sparsely populated, high dimensional feature space
  - n Each point (unit in the fleet) has a record in a DB, describing model, configuration, operational and maintenance information
  - n Each point has a collective of peers
  - n *Collective of peers* are units whose individual experience can be composed to better predict the unit's performance
  - n To adapt to changes in units or peers, we will re-assess the collective over time



# Metric of Success: Selection Precision



# Asset Selection Outline

- Problem Description
- **Data Collection and Experiments Set-Up**
  - *Data Sources*
  - *Experiments: Metrics and Baselines*
- Proposed Peer-Learning Methodology
- Results
- Conclusions

# Data Compilation and Experiments

## Data Categories:

- Configuration Information *(Source: GE Rail)*
- Maintenance & Repair Information
  - Fault Codes *(Source: Locomotive's EOA)*
  - Recommendations *(Source: GE Rail)*
  - Repairs *(Source: GE Rail / Railroads)*
- Utilization Information *(Source: Railroads)*

### Locomotives with EOA Service



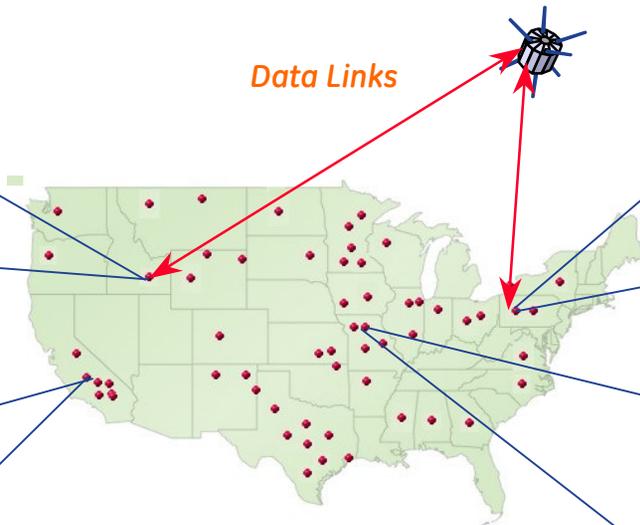
**Fault codes**  
*(3 uploads/day)*

### Railroad Yards



**Utilization Information**  
*(1 download/~ 30 days)*

*Data Links*



### GE Rail Locomotives Services



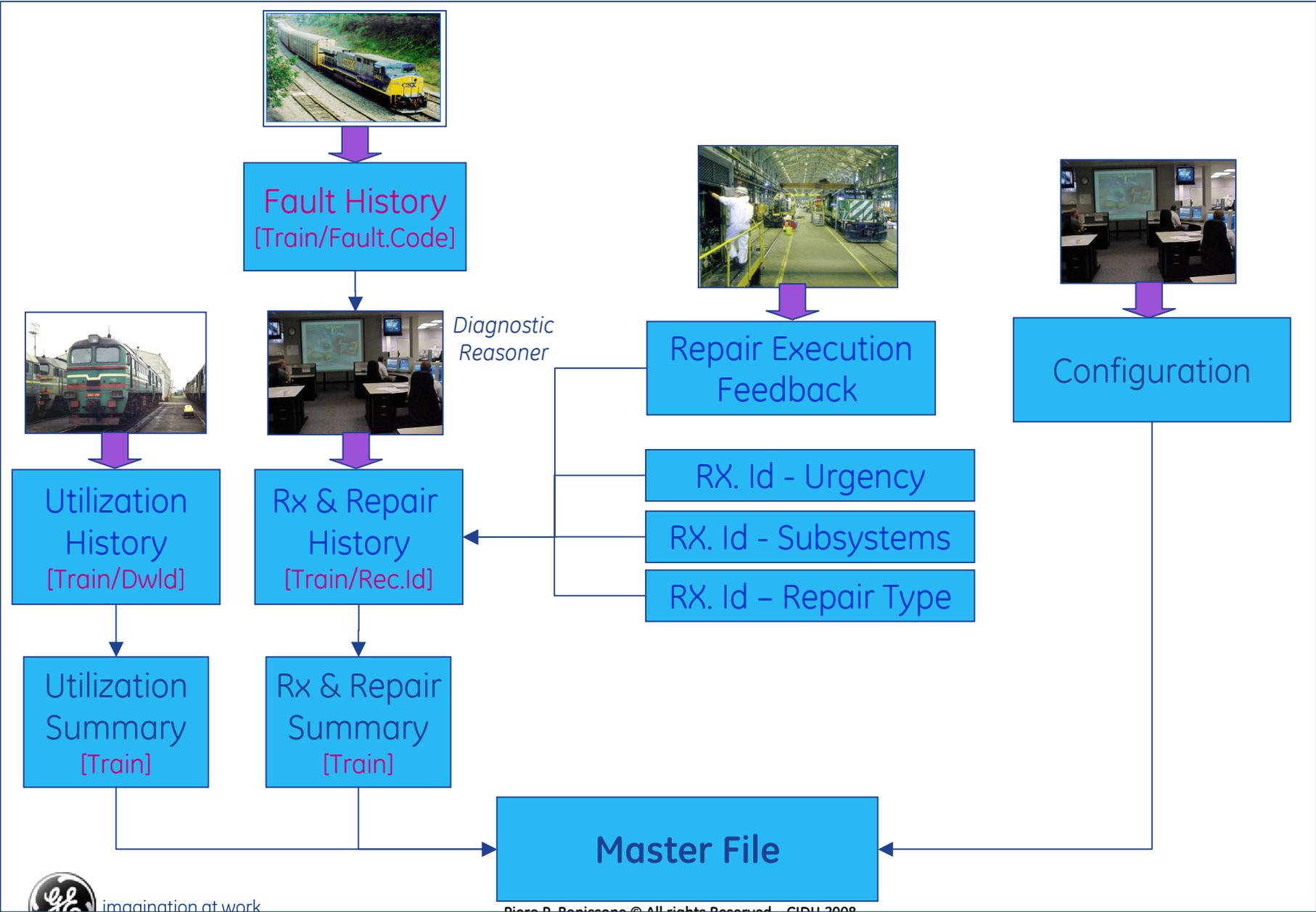
**Recommendations**  
*(4-8 Rx/yr)*

### GE Rail/Railroads Repair Shops

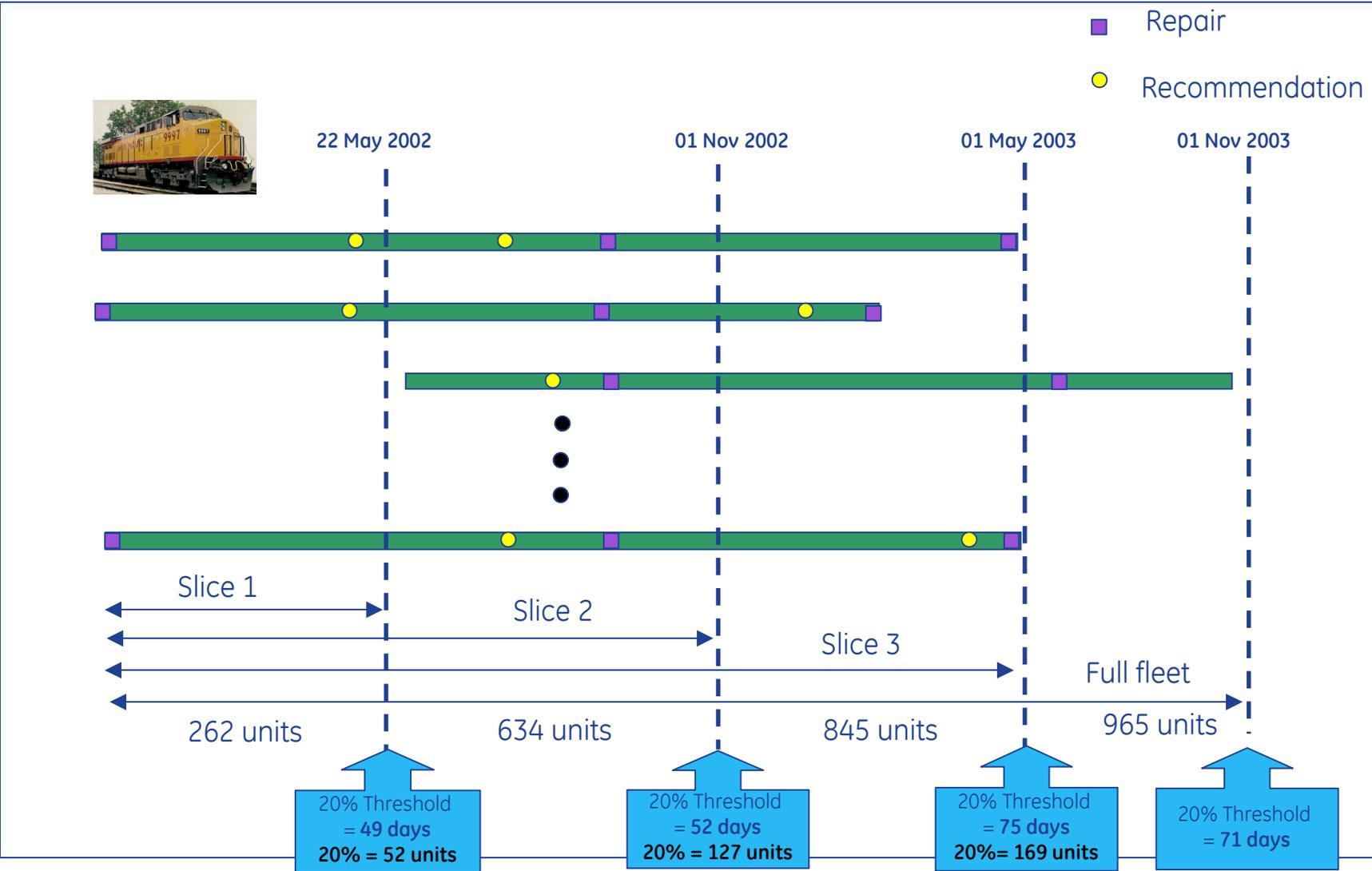


**Repair Execution**  
*(4-8 Repairs/yr)*

# Data Collection and Compilation: Tables Relationships



# Data Slices



# Asset Selection Outline

- Problem Description
- Data Collection and Experiments Set-Up
- **Proposed Peer-Learning Methodology**
  - *Definition of Peers*
  - *Fuzzy Instance-based Classifier (FIBC)*
  - *Evolution of FIBC Design*
- Results
- Conclusions

# Current Location of All Available Locomotives

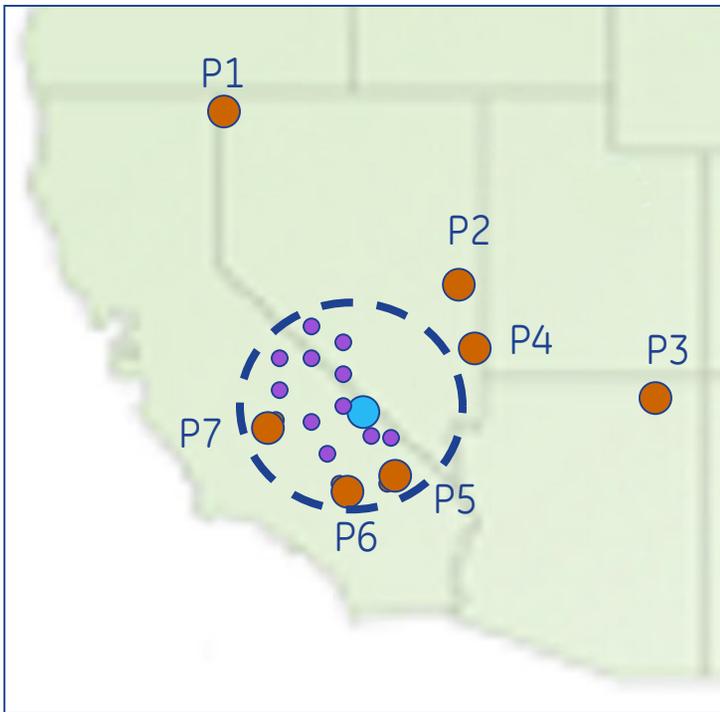


## Mission Requirements

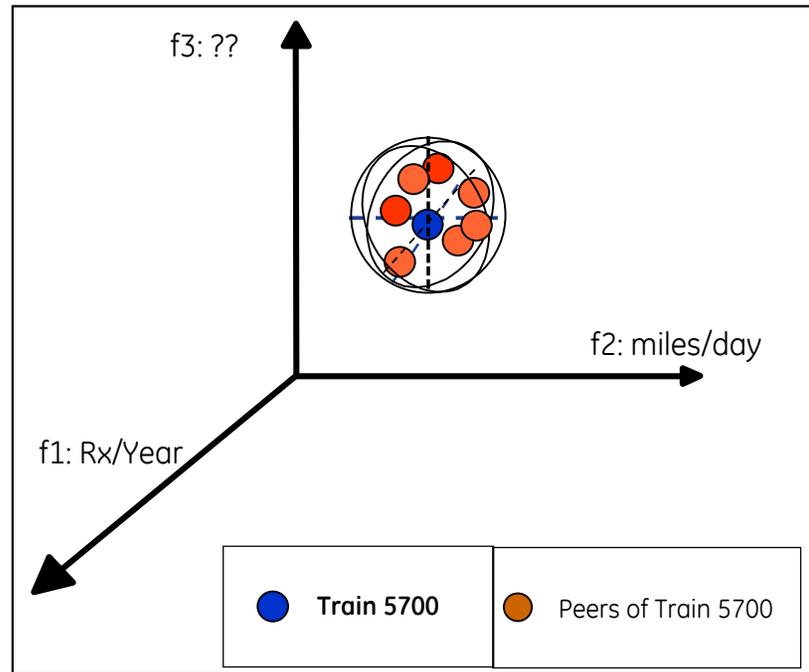
# Locomotives needed:	12
Duration:	9 days
Start date:	+ 48 hrs
Distance:	2,435 miles
Average Miles/day	304 m/day Max
Grade/Elevation:	2%
Climate, Tunnel operation:	desert, hot

<b>Loco Number:</b>	<b>5700</b>
<b>Design and Configuration</b>	
Type:	<b>AC4400</b>
Electrical System:	<b>Bosch</b>
...	
<b>Utilization Information</b>	
Age:	<b>2.9 years</b>
Mileage:	<b>247,567 mi.</b>
Average miles/day:	<b>299</b>
<b>Maintenance Information</b>	
Time elapsed since last repair:	<b>10 days</b>
Median time between repairs	<b>60 days</b>
Median time from repair to next recommendation (Rx)	<b>52 days</b>

# Identifying Loco 5700's Peers



● = Peers of Loco 5700



Experiments focused on defining the relevant attributes ( $f1, f2, \dots, fn$ ) for defining peers

The cluster of peers defines the *collective* for this unit

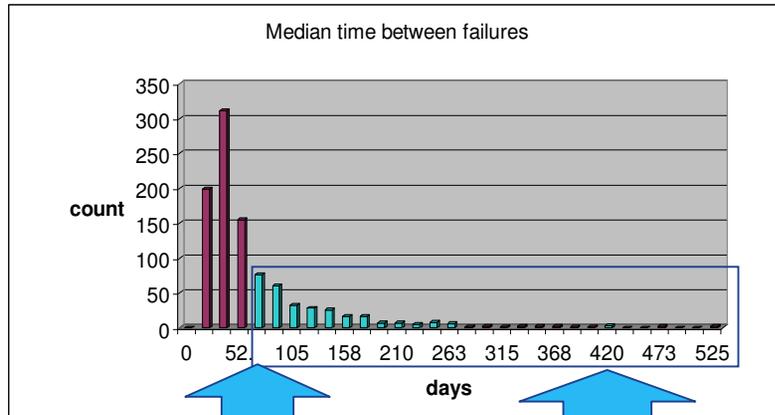
# Asset Selection Outline

- Problem Description
- Data Collection and Experiments Set-Up
- Proposed Peer-Learning Methodology
- **Results**
  - *Experiment 1: Top 20% Current Performers*
    - *Robustness*
  - *Experiment 2: Top 52 units Current Performers*
  - *Experiment 3: Top 20% Future Performers*
  - *Experiment 3 bis: Top 20% Future Performers*
    - *Static vs Dynamic Models*
- Conclusions

# Baseline – Single-Heuristic based Selection

- Heuristic selection of N1 units (based on full fleet)

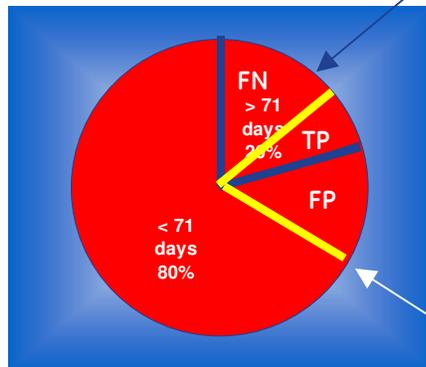
Objective: Create heuristic knowledge driven baseline.



Target: time between failures > 71 days

Random selection in target area: ~20%

Ground Truth



Ground Truth	T	F
Predicted	T	F
	TP	FP
	F	TN
	FN	TN

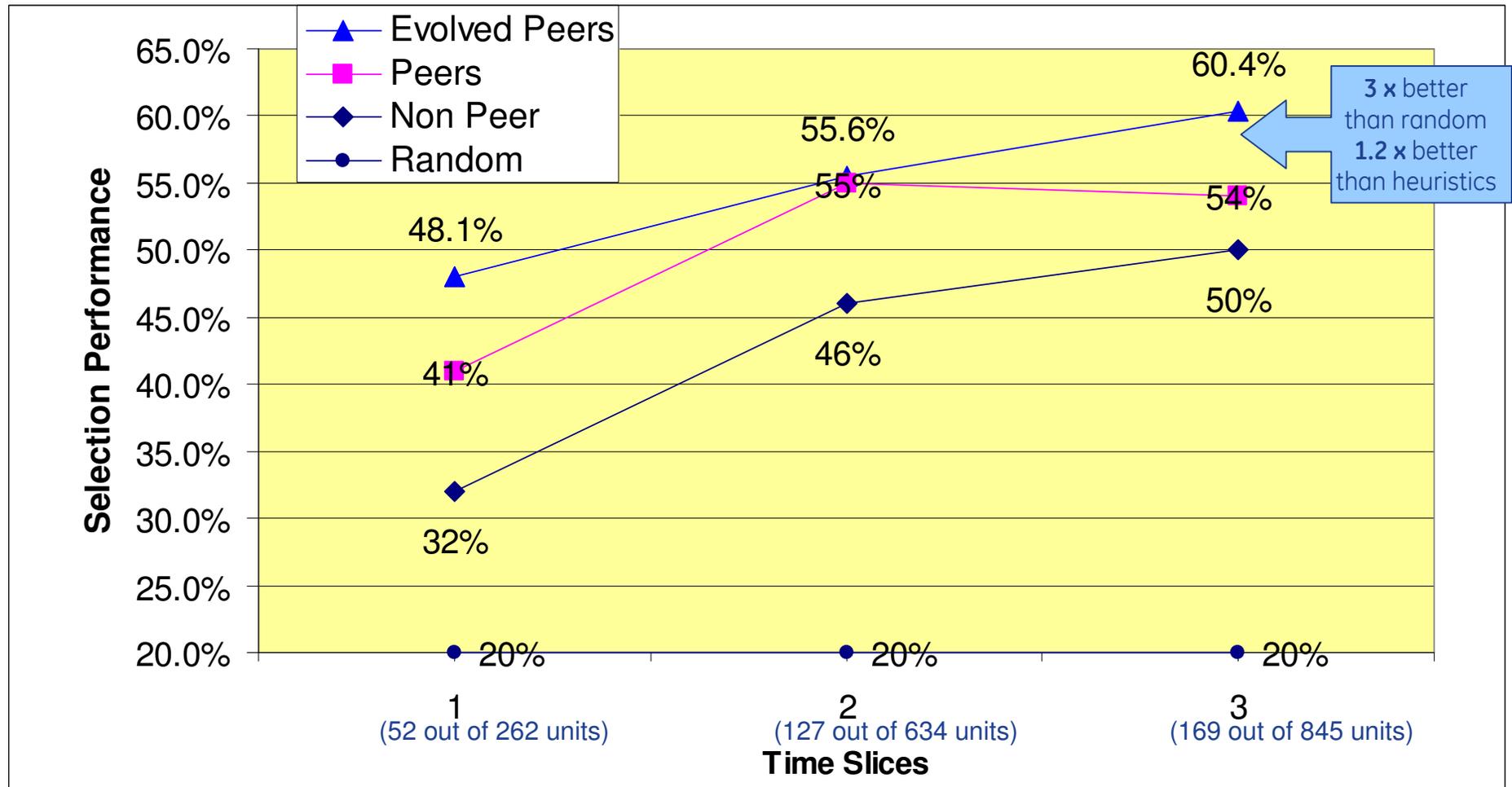
Predicted

Single Heuristic	% of Correctly Classified Units = TP/20%	% Data Correct
Lowest Mileage	17%	81%
Newest Units	18%	100%
Random	20%	N/A
Highest Energy (MWHRS) generated	24%	79%
Highest Miles/ Hours Moving	26%	97%
Highest Percentage Hours Moving	29%	58%
Lowest Percentage of: Subsystem 10 Failures	38%	95%
Lowest Ratio: Recommendations / Age [Rx/yr]	49%	100%



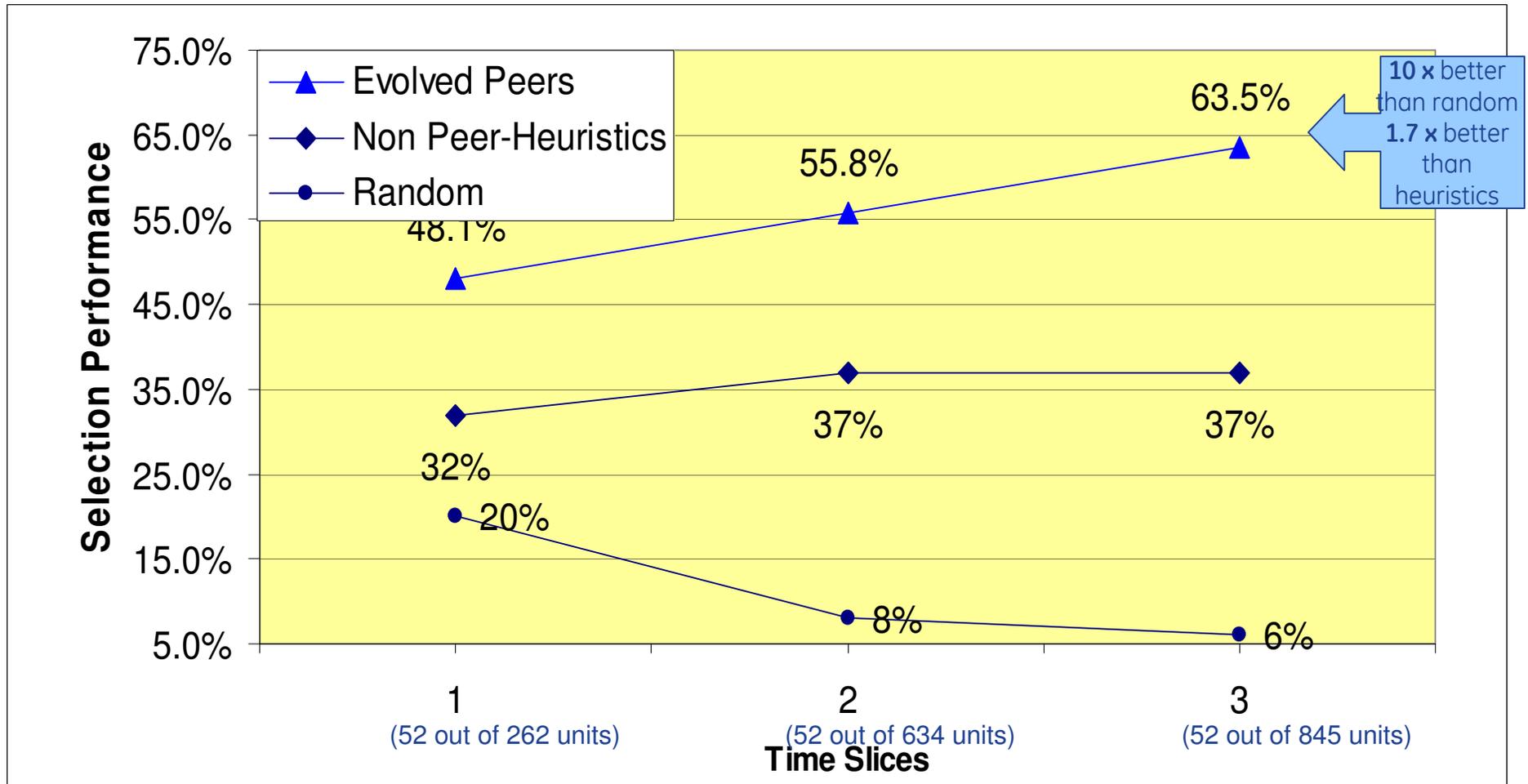
imagination at work

# Exp 1: Peers Evolution over Time: Estimating Best Current performers (20%)



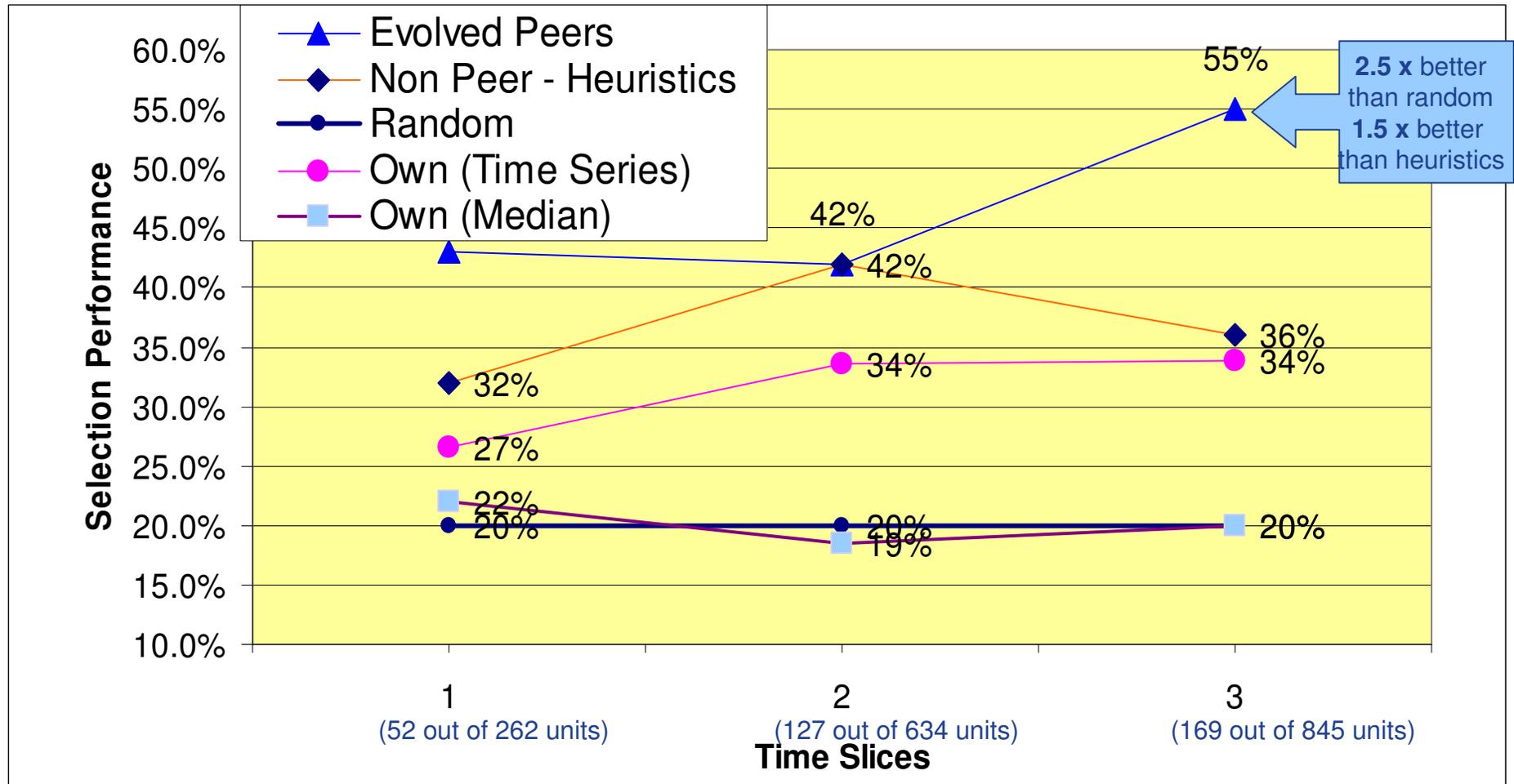
(Targeting top 20% of units for each Time Slice)

# Exp 2: Peers Evolution over Time: Estimating best Current performers (52 units)



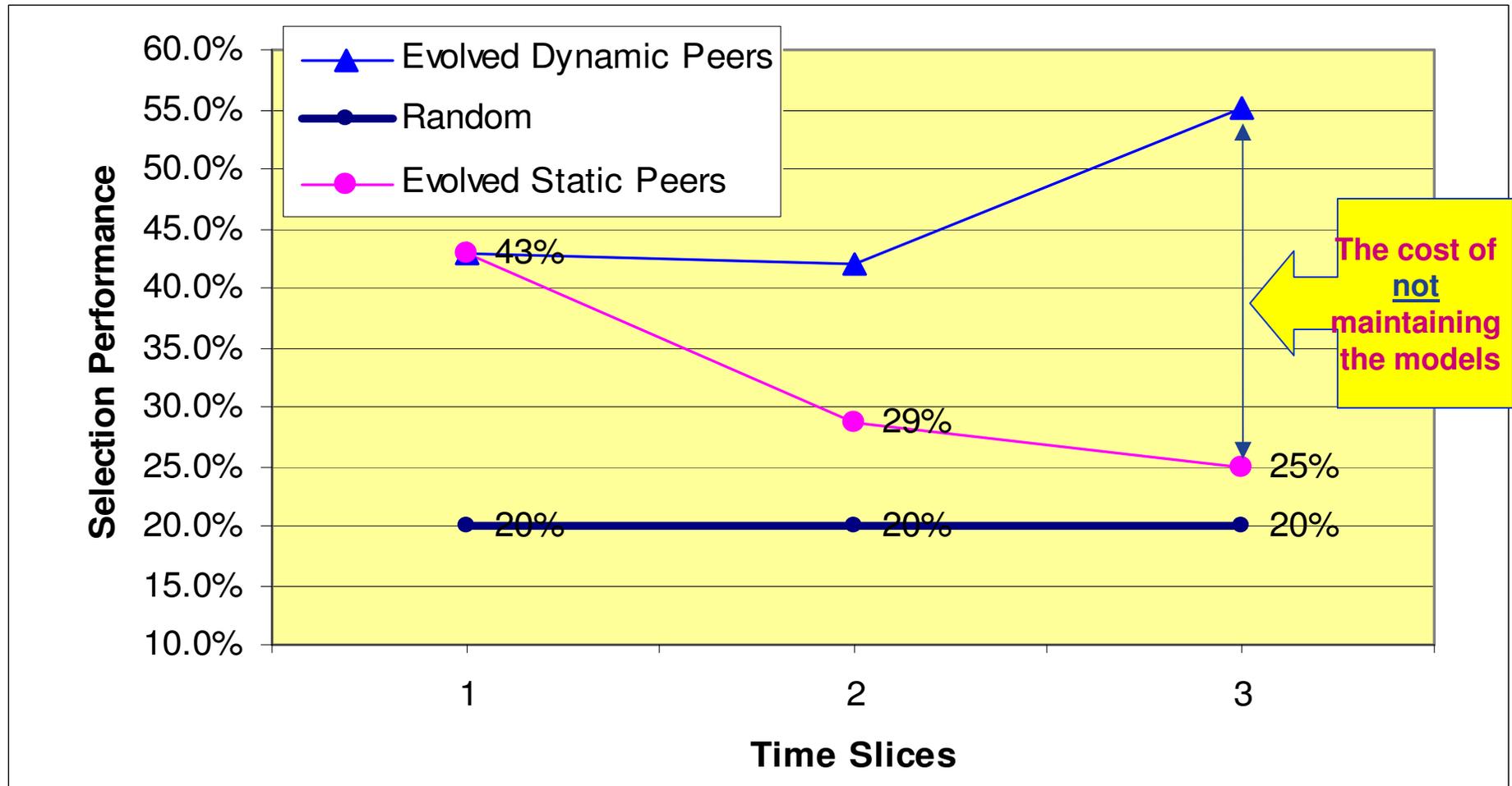
(Targeting Top 52 units for each Time Slice)

# Exp 3: Peers Evolution over Time: Estimating best future performers



(Targeting top 20% of units for each Time Slice)

# Experiment 4: Comparing Evolved, Dynamic (updated) Peers with Evolved Static (Non-updated) Peers: Estimating Best Future Performers



The Benefit of Automated Peer Redesign/Update



# Asset Selection Outline

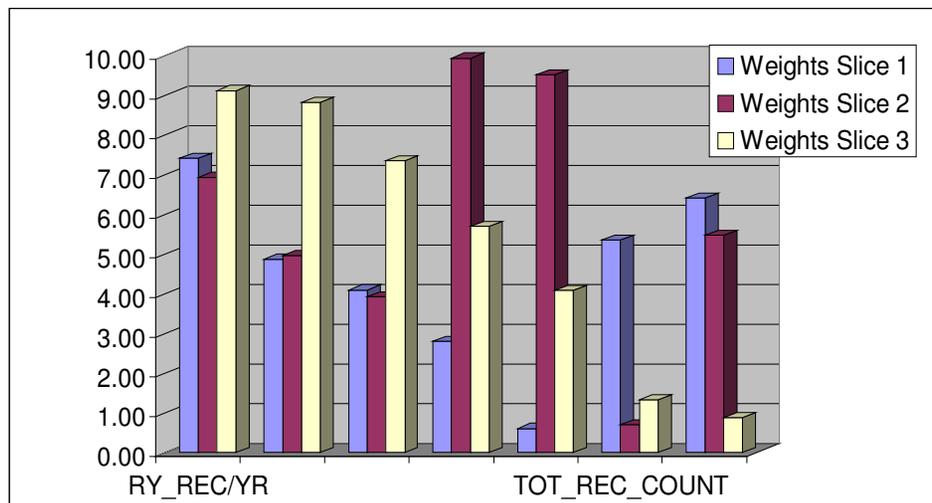
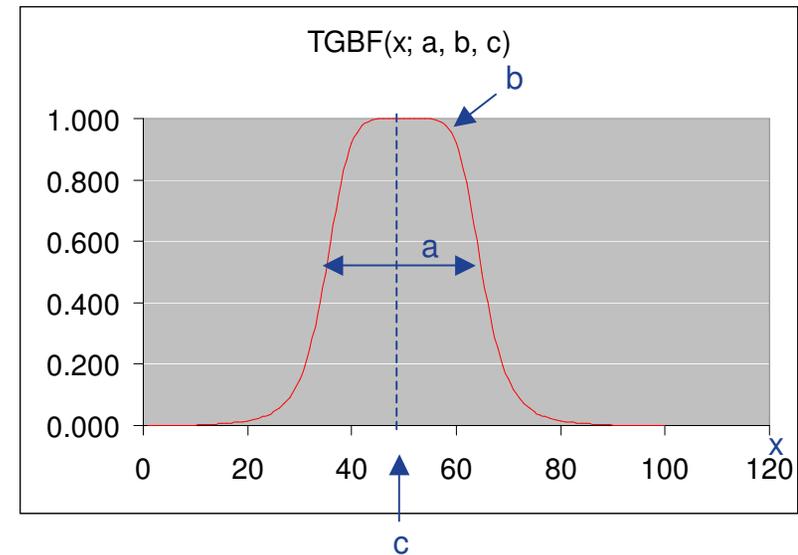
- Problem Description
- Data Collection and Experiments Set-Up
- Proposed Peer-Learning Methodology
- Results
- **Conclusions**
  - *Summary*



To Future Work.

# Attribute Weighing using GA [Slice 3] (for prediction, ranking, and selection of best units)

Feature	Weight	a	b
RY_REC/YR	9.11	5.55	3.73
RY_REC/100K_MILES	8.81	5.35	2.57
RY_REC/100K_ENGINE_HRS	7.35	35.94	2.67
REC_COUNT_RY	5.69	8.49	3.37
RY_REC/100K_ENG_HRS_MOVE	4.08	10.06	2.75
TOT_REC_COUNT	1.33	18.70	3.20
RED_REC_COUNT	0.87	0.99	3.16



$$TGBF = \begin{cases} \frac{1}{1 + \left| \frac{x - c}{a} \right|^{2b}} & \text{if } GBF > 10^{-5} \\ 0 & \text{otherwise} \end{cases}$$

# Conclusions

- **Validating the Premise**

- Combining limited utilization and maintenance history **improves our ability to select the best units for a mission.**
- Evolved Peers provided the **best overall accuracy** (60.35% = over 3 times better than random selection) for past performance. When the selection was limited to a small fixed number of units, Evolved Peers provided an accuracy of 63.5% (**over 10 times better than random selection**) for past performance.
- Evolved Peers provided the **best overall accuracy** (55% = **2.7 times better than random selection** and 1.5 x better than best heuristics) for future performance
- Construction of local fuzzy models does not require computing a distance in the n-dimensional feature space

- **Operational Impact:**

- **Robustness** to information loss exhibited by peer-based approach will enable mission reliability for minimally instrumented platforms operating with limited bandwidth



## 6. Future Work

- Improving the Feature Space: GP for Attribute Construction
- Improving Fitness Function: Accuracy, Confidence, Info. Theory
- Improving Aggregation: Adapting Kernel Based Regressions

# Future Work

- **Extend evolutionary search**
  - from attribute selection and weighting to attribute construction
- **Improve fitness function**
  - to address classifier accuracy and confidence, and representation parsimony
- **Improve aggregation models**



[To References](#)

# Future Work

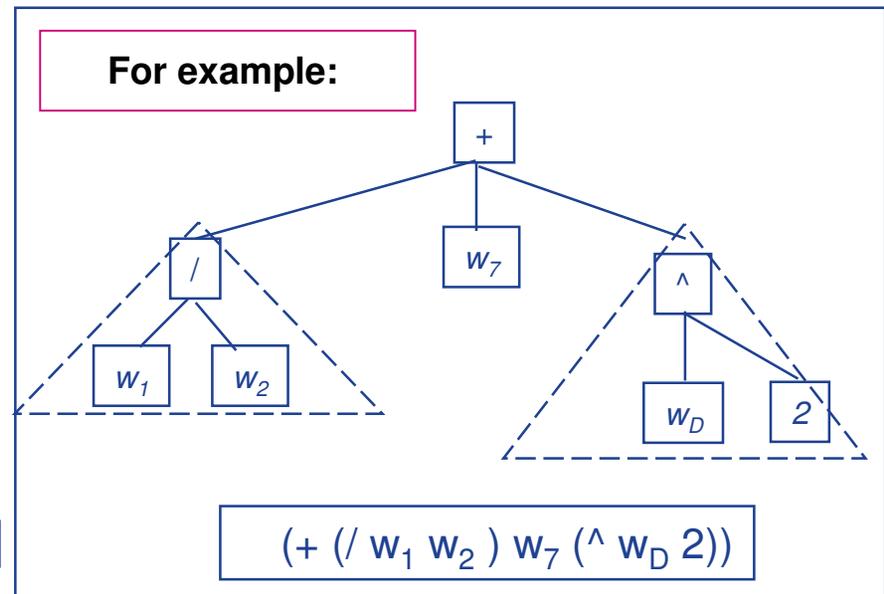
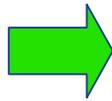
- Extend evolutionary search from attribute selection and weighting to *attribute construction*.

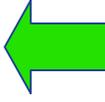
Use **Genetic Programming** to automate attribute construction and evolve attribute space with functional compositions of primitive attributes

**GA:**  $[(w_1, w_2, \dots, w_D)] [(a_1, b_1), \dots, (a_D, b_D)] [\alpha]$  

**GP:**  $[f_1 * g_1 * \dots * h_1(w_1, w_2, \dots, w_D), \dots, f_D * g_D * \dots * h_D(w_1, w_2, \dots, w_D)] [(a_1, b_1), \dots, (a_D, b_D)] [\alpha]$

A sentence derived from a grammar that defines a syntactically correct functional composition of attributes to replace a primitive attribute



$\left( \frac{w_1}{w_2} + w_7 + w_D^2 \right)$  

# Future Work: Improving the Fitness Function

- Extend evolutionary search.
- Improve *fitness function* to address classifier accuracy and confidence, and representation parsimony

classifier accuracy, confidence and representation parsimony

$$f1 = \alpha_1 \left[ \frac{\text{TotPred} - \text{CorrPred}}{\text{TotPred}} \right] + \alpha_2 \left[ \frac{\sum_{i=1}^{\text{TotPred}} \frac{n \min_i}{K_i}}{\text{TotPred}} \right] + \alpha_3 \left| \frac{\left( \sum_{j=1}^D w_j \right) - 1}{(D-1)} \right| =$$

$$= \alpha_1 [\text{Classifier\_Inaccuracy}] + \alpha_2 [\text{Average}(\text{Retrieval\_Inaccuracy})] + \alpha_3 \left| \frac{d-1}{D-1} \right|$$

Predicted →	T	F
Ground Truth ↓		
T	TP	FP
F	FN	TN

Assumptions:

Two-class problem or

Multiple class problem with indistinguishable errors

Where:

$$\text{Classifier\_Inaccuracy} = (\text{FN} + \text{FP}) / (\text{TP} + \text{FP} + \text{FN} + \text{TN})$$

$$\text{TotPred} = (\text{TP} + \text{FP} + \text{FN} + \text{TN})$$

$n \min_i$  = number of minority decisions in  $i^{\text{th}}$  retrieval

$K_i$  = number of points retrieved for case  $I$  (Cardinality of  $i^{\text{th}}$  retrieval)

$\text{Retrieval\_Inaccuracy}(i) = (n \min_i) / K_i = \text{Cardinality of Non-Mode} / \text{TotalCardinality}$  for  $i^{\text{th}}$  retrieval

Typical values:  $\alpha_1 = 2$ ;  $\alpha_2 = 0.2$ ;  $\alpha_3 = 0.1$



# Future Work

- Extend evolutionary.
- Improve *fitness function*
- **Improve aggregation models**

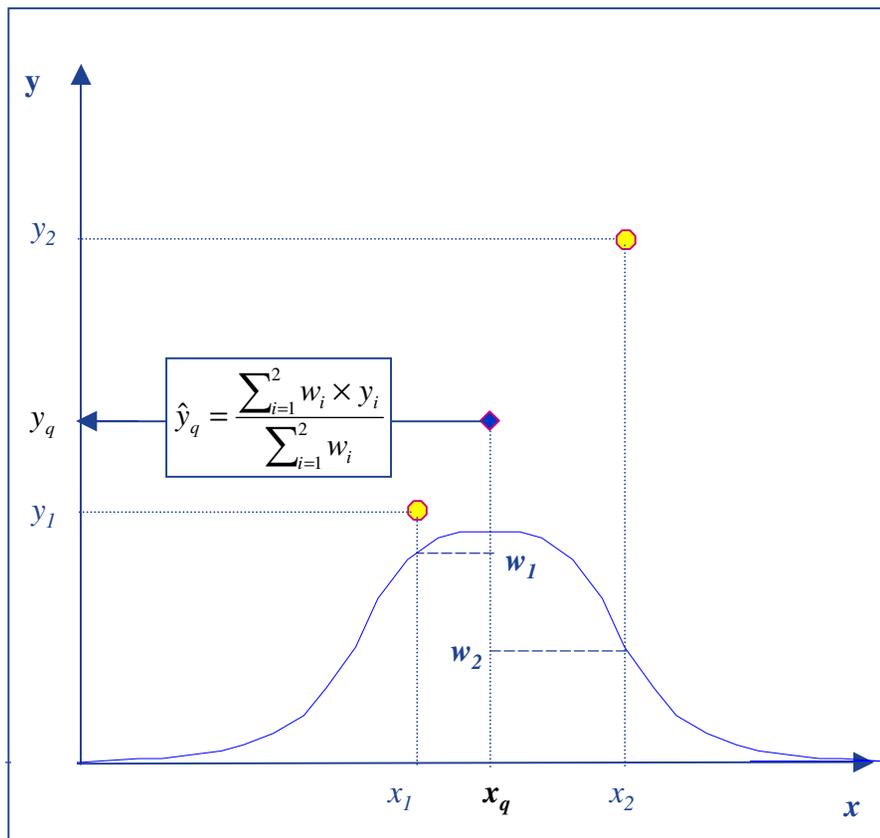
We could use the similarity measures as ***kernel functions*** for each dimension  $i$  and create ***kernel-based regressions***

We would use local search methods to obtain the parameters of the kernel-based regression, within each trial of the EA's.

# Future Work: Improving Aggregation

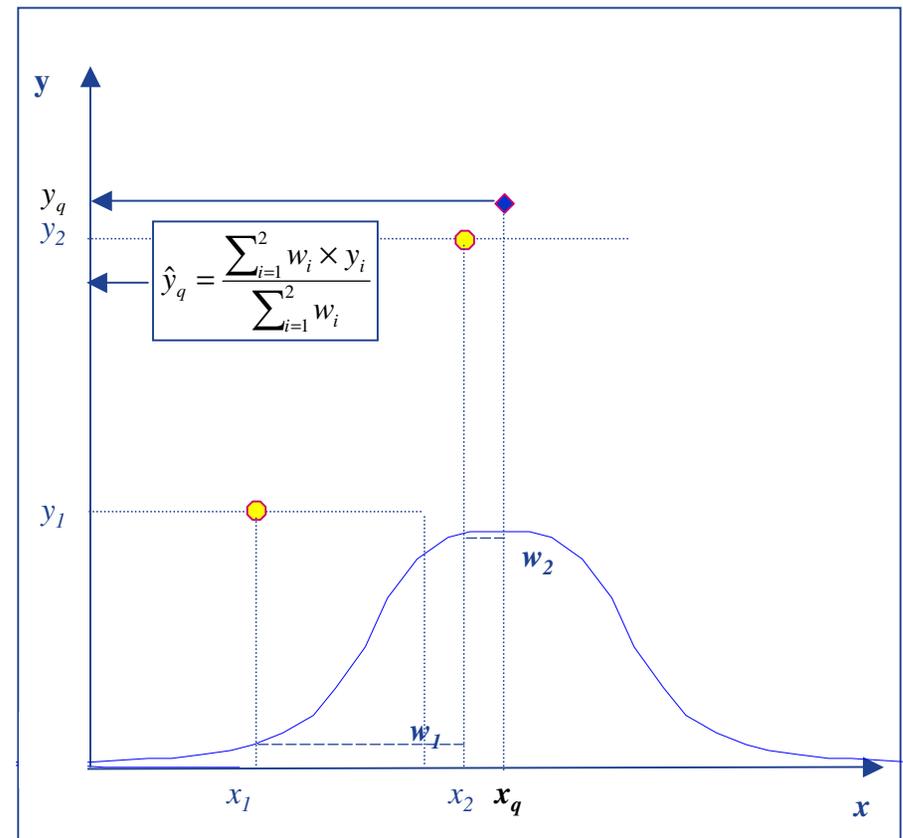
0<sup>th</sup> Order Approximation (weighted average)

- It works well when **interpolating**



0<sup>th</sup> Order Approximation (weighted average)

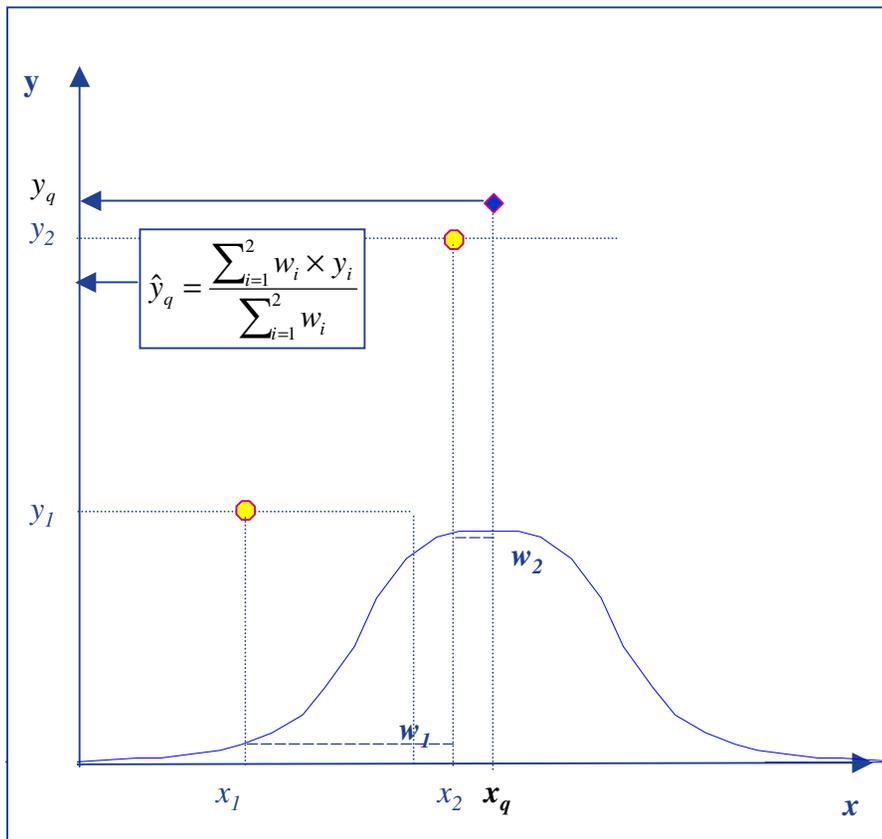
- It is lousy when **extrapolating**
- Bounded by the **minimum & maximum** of its arguments



# Future Work: Improving Aggregation

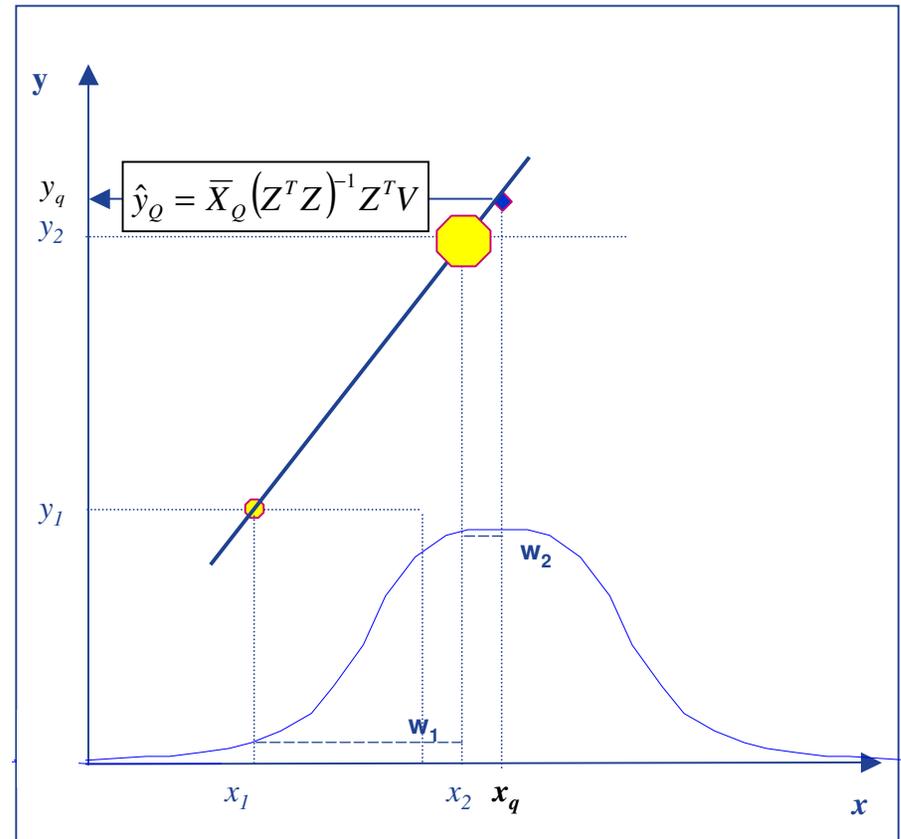
**0<sup>th</sup> Order Approximation** (weighted average)

- It is lousy when **extrapolating**
- Bounded by the **minimum & maximum** of its arguments

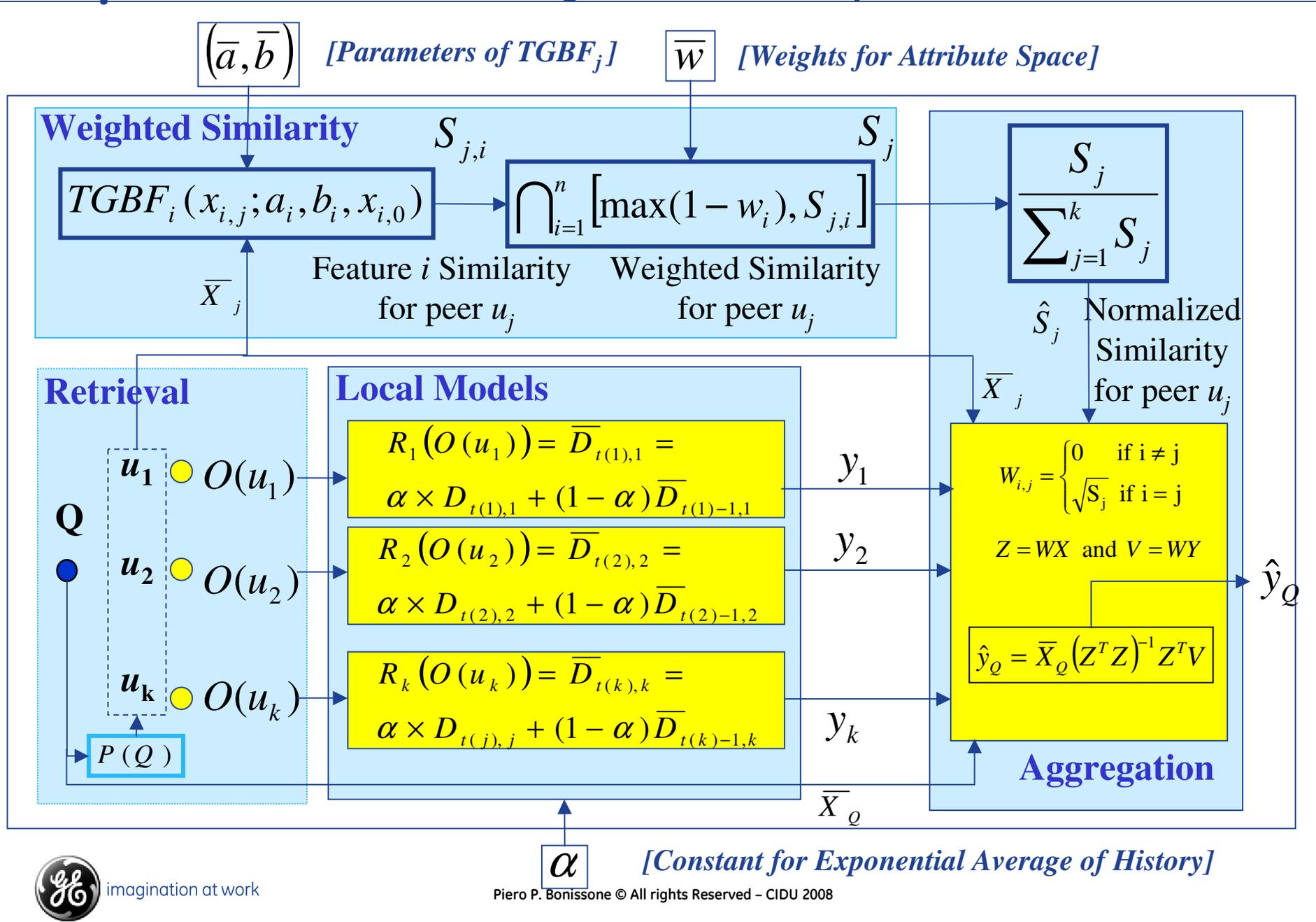


**1<sup>st</sup> Order Approximation** (Weighted Linear Regression)

- Weight each data point by its similarity degree with the probe Q



# Improved F-IBM: Algebraic Interpretation



# Further Resources

From my Web site:

[www.rpi.edu/~bonisp](http://www.rpi.edu/~bonisp)

Go to:

<http://www.rpi.edu/~bonisp/publications-new.html>

## Relevant papers that you can download:

"Hybrid Soft Computing Systems: Industrial and Commercial Applications", P. P. Bonissone, Y-T Chen, K. Goebel and P. S. Khedkar, *Proceedings of the IEEE*, pp 1641--1667, vol. 87, no. 9, Sept. 1999. <http://www.rpi.edu/~bonisp/NASA-course/hybridSC99.pdf>

"When will it break? A Hybrid Soft Computing Model to Predict Time-to-break Margins in Paper Machines", P. Bonissone and K. Goebel, *Proc. SPIE 2002*, pp. 53--64, Aug. 2002, Seattle, WA <http://www.rpi.edu/~bonisp/NASA-course/webbreakage.pdf>

"Evolutionary Optimization of Fuzzy Decision Systems for Automated Insurance Underwriting", P. Bonissone, R. Subbu, and K. Aggour, *Proc. FUZZ-IEEE 2002*, pp. 1003 - 1008, May 2002, Honolulu, HI. <http://www.rpi.edu/~bonisp/NASA-course/wcci2002.pdf>

"Automating the Quality Assurance of an On-line Knowledge-Based Classifier By Fusing Multiple Off-line Classifiers", P. Bonissone, *Inform. Proc. & Management of Uncertainty (IPMU)*, Perugia, Italy, July 2004 <http://www.rpi.edu/~bonisp/NASA-course/IPMUv8.pdf>

"Development and Maintenance of Fuzzy Models in Financial Applications", P. Bonissone, *Proc. SMPS 2004*, Oviedo, Spain, September 2004. <http://www.rpi.edu/~bonisp/NASA-course/Oviedo2004.pdf>

"Six Sigma Quality Applied Throughout the Lifecycle of and Automated Decision System", A. Patterson, P. Bonissone, and M. Pavese, *Journal of Quality and Reliability International*, 21:275-292, 2005 <http://www.rpi.edu/~bonisp/NASA-course/SixSigma.pdf>

"An Evolutionary Process for Designing and Maintaining a Fuzzy Instance-based Model (FIM)", P. Bonissone, A. Varma, K. Aggour, *1st Workshop Genetic Fuzzy Systems (GFS 2005)*, Granada, Spain, March 2005. <http://www.rpi.edu/~bonisp/NASA-course/piero-gfsmod.pdf>

"Predicting the Best Units within a Fleet: Prognostic Capabilities Enabled by Peer Learning, Fuzzy Similarity, and Evolutionary Design Process", P. Bonissone, A. Varma, *FUZZ-IEEE 2005*, pp 312-318, Reno NV, May 22-25, 2005.

<http://www.rpi.edu/~bonisp/NASA-course/fuzz05anilfinalv27.pdf>



imagination at work

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# Questions ?

Thank You!



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